aroma.light

November 11, 2009

${\sf R}$ topics documented:

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1. Calibration and Normalization

1. Calibration and Normalization

Description

In this section we give *our* recommendation on how spotted two-color (or multi-color) microarray data is best calibrated and normalized.

Classical background subtraction

We do *not* recommend background subtraction in classical means where background is estimated by various image analysis methods. This means that we will only consider foreground signals in the analysis.

We estimate "background" by other means. In what is explain below, only a global background, that is, a global bias, is estimated and removed.

Multiscan calibration

In Bengtsson et al (2004) we give evidence that microarray scanners can introduce a significant bias in data. This bias, which is about 15-25 out of 65535, *will* introduce intensity dependency in the log-ratios, as explained in Bengtsson & Hössjer (2006).

In Bengtsson et al (2004) we find that this bias is stable across arrays (and a couple of months), but further research is needed in order to tell if this is true over a longer time period.

To calibrate signals for scanner biases, scan the same array at multiple PMT-settings (in decreasing order) at three or more PMT settings. Do this *without* washing, cleaning or by other means changing the array between subsequent scans. Although not necessary, it is preferred that the array remains in the scanner between subsequent scans. This will simplify the image analysis since spot identification can be made once if images aligns perfectly.

After image analysis, read all K scans for the same array into the two matrices, one for the red and one for the green channel, where the K columns corresponds to scans and the N rows to the spots. It is enough to use foreground signals.

In order to multiscan calibrate the data, for each channel separately call Xc <- calibrate Multiscan(X) where X is the NxK matrix of signals for one channel across all scans. The calibrated signals are returned in the Nx1 matrix Xc.

Multiscan calibration may sometimes be skipped, especially if affine normalization is applied immediately after, but we do recommend that every lab check at least once if their scanner introduce bias.

Affine normalization

In Bengtsson & Hössjer (2006), we carry out a detailed study on how biases in each channel introduce so called intensity-dependent log-ratios among other systematic artifacts. Data with (additive) bias in each channel is said to be *affinely* transformed. Data without such bias, is said to be *linearly* (proportionally) transform. Ideally, observed signals (data) is a linear (proportional) function of true gene expression levels.

We do *not* assume proportional observations. The scanner bias is real evidence that assuming linearity is not correct. Affine normalization corrects for affine transformation in data. Without control spots it is not possible to estimate the bias in each of the channels but only the relative bias

such that after normalization the effective bias are the same in all channels. This is why we call it normalization and not calibration.

In its simplest form, affine normalization is done by Xn < - normalizeAffine(X) where X is a Nx2 matrix with the first column holds the foreground signals from the red channel and the second holds the signals from the green channel. If three- or four-channel data is used these are added the same way. The normalized data is returned as a Nx2 matrix Xn.

To normalize all arrays and all channels at once, one may put all data into one big NxK matrix where the K columns hold the all channels from the first array, then all channels from the second array and so on. Then Xn < - normalizeAffine(X) will return the across-array and across-channel normalized data in the NxK matrix Xn where the columns are stored in the same order as in matrix X.

Equal effective bias in all channels is much better. First of all, any intensity-dependent bias in the log-ratios is removed *for all non-differentially expressed genes*. There is still an intensity-dependent bias in the log-ratios for differentially expressed genes, but this is now symmetric around log-ratio zero.

Affine normalization will (by default and recommended) normalize *all* arrays together and at once. This will guarantee that all arrays are "on the same scale". Thus, it *not* recommended to apply a classical between-array scale normalization afterward. Moreover, the average log-ratio will be zero after an affine normalization.

Note that an affine normalization will only remove curvature in the log-ratios at lower intensities. If a strong intensity-dependent bias at high intensities remains, this is most likely due to saturation effects, such as too high PMT settings or quenching.

Note that for a perfect affine normalization you *should* expect much higher noise levels in the *log-ratios* at lower intensities than at higher. It should also be approximately symmetric around zero log-ratio. In other words, *a strong fanning effect is a good sign*.

Due to different noise levels in red and green channels, different PMT settings in different channels, plus the fact that the minimum signal is zero, "odd shapes" may be seen in the log-ratio vs log-intensity graphs at lower intensities. Typically, these show themselves as non-symmetric in positive and negative log-ratios. Note that you should not see this at higher intensities.

If there is a strong intensity-dependent effect left after the affine normalization, we recommend, for now, that a subsequent curve-fit or quantile normalization is done. Which one, we do not know.

Why negative signals? By default, 5% of the normalized signals will have a non-positive signal in one or both channels. *This is on purpose*, although the exact number 5% is chosen by experience. The reason for introducing negative signals is that they are indeed expected. For instance, when measure a zero gene expression level, there is a chance that the observed value is (should be) negative due to measurement noise. (For this reason it is possible that the scanner manufacturers have introduced scanner bias on purpose to avoid negative signals, which then all would be truncated to zero.) To adjust the ratio (or number) of negative signals allowed, use for example normalizeAffine(X, constraint=0.01) for 1% negative signals. If set to zero (or "max") only as much bias is removed such that no negative signals exist afterward. Note that this is also true if there were negative signals on beforehand.

Why not lowess normalization? Curve-fit normalization methods such as lowess normalization are basically designed based on linearity assumptions and will for this reason not correct for channel biases. Curve-fit normalization methods can by definition only be applied to one pair of channels at the time and do therefore require a subsequent between-array scale normalization, which is by the way very ad hoc.

Why not quantile normalization? Affine normalization can be though of a special case of quantile normalization that is more robust than the latter. See Bengtsson & Hössjer (2006) for details. Quantile normalization is probably better to apply than curve-fit normalization methods, but less

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robust than affine normalization, especially at extreme (low and high) intensities. For this reason, we do recommend to use affine normalization first, and if this is not satisfactory, quantile normalization may be applied.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

```
aroma.light-package
```

Package aroma.light

Description

Methods for microarray analysis that take basic data types such as matrices and lists of vectors. These methods can be used standalone, be utilized in other packages, or be wrapped up in higher-level classes.

Requirements

This package requires the **R.oo** package [1].

Installation

To install this package, see http://www.braju.com/R/. Required packages are installed in the same way.

To get started

For scanner calibration:

1. see calibrateMultiscan.matrix() - scan the same array two or more times to calibrate for scanner effects and extended dynamical range.

To normalize multiple single-channel arrays all with the same number of probes/spots:

- 1. normalizeAffine.matrix() normalizes, on the intensity scale, for differences in offset and scale between channels.
- 2. normalizeQuantileRank.matrix(), normalizeQuantileSpline.matrix() normalizes, on the intensity scale, for differences in empirical distribution between channels.

To normalize multiple single-channel arrays with varying number probes/spots:

1. normalizeQuantileRank.list(), normalizeQuantileSpline.list() - normalizes, on the intensity scale, for differences in empirical distribution between channels.

To normalize two-channel arrays:

- 1. normalizeAffine.matrix() normalizes, on the intensity scale, for differences in offset and scale between channels. This will also correct for intensity-dependent affects on the log scale.
- 2. normalizeCurveFit.matrix() Classical intensity-dependent normalization, on the log scale, e.g. lowess normalization.

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To normalize three or more channels:

1. normalizeAffine.matrix() - normalizes, on the intensity scale, for differences in offset and scale between channels. This will minimize the curvature on the log scale between any two channels.

Further readings

Several of the normalization methods proposed in [3]-[6] are available in this package.

How to cite this package

Whenever using this package, please cite [2] as

No citation information available.

Wishlist

Here is a list of features that would be useful, but which I have too little time to add myself. Contributions are appreciated.

• At the moment, nothing.

If you consider to contribute, make sure it is not already implemented by downloading the latest "devel" version!

License

The releases of this package is licensed under LGPL version 2.1 or newer.

The development code of the packages is under a private licence (where applicable) and patches sent to the author fall under the latter license, but will be, if incorporated, released under the "release" license above.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

Some of the reference below can be found at http://www.maths.lth.se/bioinformatics/publications/.

- [1] H. Bengtsson, *The R.oo package Object-Oriented Programming with References Using Standard R Code*, In Kurt Hornik, Friedrich Leisch and Achim Zeileis, editors, Proceedings of the 3rd International Workshop on Distributed Statistical Computing (DSC 2003), March 20-22, Vienna, Austria. http://www.ci.tuwien.ac.at/Conferences/DSC-2003/Proceedings/
- [2] H. Bengtsson, *aroma An R Object-oriented Microarray Analysis environment*, Preprints in Mathematical Sciences (manuscript in preparation), Mathematical Statistics, Centre for Mathematical Sciences, Lund University, 2004.
- [3] Henrik Bengtsson and Ola Hössjer, *Methodological Study of Affine Transformations of Gene Expression Data*, Methodological study of affine transformations of gene expression data with proposed robust non-parametric multi-dimensional normalization method, BMC Bioinformatics, 2006,

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7:100.

[4] H. Bengtsson, J. Vallon-Christersson and G. Jönsson, *Calibration and assessment of channel-specific biases in microarray data with extended dynamical range*, BMC Bioinformatics, 5:177, 2004.

[5] H. Bengtsson, R. Irizarry, B. Carvalho, and T. Speed, *Estimation and assessment of raw copy numbers at the single locus level*, Bioinformatics, 2008.

[6] H. Bengtsson, *Identification and normalization of plate effects in cDNA microarray data*, Preprints in Mathematical Sciences, 2002:28, Mathematical Statistics, Centre for Mathematical Sciences, Lund University, 2002.

```
averageQuantile.list
```

Gets the average empirical distribution

Description

Gets the average empirical distribution for a set of samples of different sizes.

Usage

```
## S3 method for class 'list':
averageQuantile(X, ...)
```

Arguments

X a list with numeric vectors. The vectors may be of different lengths.

... Not used.

Value

Returns a numeric vector of length equal to the longest vector in argument X.

Missing values

Missing values are excluded.

Author(s)

Parts adopted from Gordon Smyth (http://www.statsci.org/) in 2002 & 2006. Original code by Ben Bolstad at Statistics Department, University of California.

See Also

```
*normalizeQuantileRank(). *normalizeQuantileSpline(). quantile.
```

```
backtransformAffine.matrix
```

Reverse affine transformation

Description

Reverse affine transformation.

Usage

```
## S3 method for class 'matrix':
backtransformAffine(X, a=NULL, b=NULL, project=FALSE, ...)
```

Arguments

а

X	An NxK matrix	containing data to	be backtransformed.
21	I III I I I I I I I I I I I I I I I I	containing data to	oc backuansioninca.

A scalar, vector, a matrix, or a list. First, if a list, it is assumed to contained the elements a and b, which are the used as if they were passed as seperate arguments. If a vector, a matrix of size NxK is created which is then filled *row by row* with the values in the vector. Commonly, the vector is of length K, which means that the matrix will consist of copies of this vector stacked on top of each other. If a matrix, a matrix of size NxK is created which is then filled *column by column* with the values in the matrix (collected column by column. Commonly, the matrix is of size NxK, or NxL with L < K and then the resulting matrix consists of copies sitting next to each other. The resulting NxK matrix is subtracted from the NxK matrix X.

b A scalar, vector, a matrix. A NxK matrix is created from this argument. For details see argument a. The NxK matrix X-a is divided by the resulting

NxK matrix.

returned (K values per data point are returned). If TRUE, the backtransformed

values " (X-a) /b" are projected onto the line L(a,b) so that all columns will be identical.

... Not used.

Value

The "(X-a)/b" backtransformed NxK matrix is returned. If project is TRUE, an Nx1 matrix is returned, because all columns are identical anyway.

Missing values

project

Missing values remain missing values. If projected, data points that contain missing values are projected without these.

See Also

For more information see matrix.

Examples

```
X <- matrix(1:8, nrow=4, ncol=2)</pre>
X[2,2] \leftarrow NA
print(X)
# Returns a 4x2 matrix
print(backtransformAffine(X, a=c(1,5)))
# Returns a 4x2 matrix
print(backtransformAffine(X, b=c(1,1/2)))
# Returns a 4x2 matrix
print(backtransformAffine(X, a=matrix(1:4,ncol=1)))
# Returns a 4x2 matrix
print(backtransformAffine(X, a=matrix(1:3,ncol=1)))
# Returns a 4x2 matrix
print (backtransformAffine (X, a=matrix(1:2,ncol=1), b=c(1,2)))
# Returns a 4x1 matrix
print(backtransformAffine(X, b=c(1,1/2), project=TRUE))
# If the columns of X are identical, and a identity
# backtransformation is applied and projected, the
# same matrix is returned.
X \leftarrow matrix(1:4, nrow=4, ncol=3)
Y <- backtransformAffine(X, b=c(1,1,1), project=TRUE)
print(X)
print(Y)
stopifnot(sum(X[,1]-Y) \le .Machine$double.eps)
# If the columns of X are identical, and a identity
# backtransformation is applied and projected, the
# same matrix is returned.
X <- matrix(1:4, nrow=4, ncol=3)</pre>
X[,2] \leftarrow X[,2]*2; X[,3] \leftarrow X[,3]*3;
print(X)
Y \leftarrow backtransformAffine(X, b=c(1,2,3))
print(Y)
Y <- backtransformAffine(X, b=c(1,2,3), project=TRUE)
stopifnot(sum(X[,1]-Y) <= .Machine$double.eps)</pre>
```

backtransformPrincipalCurve.matrix

Reverse transformation of principal-curve fit

Description

Reverse transformation of principal-curve fit.

Usage

```
## S3 method for class 'matrix':
backtransformPrincipalCurve(X, fit, dimensions=NULL, targetDimension=NULL, ...)
```

Arguments

X	An NxK matrix containing data to be backtransformed.	
fit	An MxL principal-curve fit object of class principal. curve as returned by *fitPrincipalCurve(). Typically $L=K$, but not always.	
dimensions	An (optional) subset of D dimensions all in $[1,L]$ to be returned (and backtransform).	
targetDimension		
	An (optional) index specifying the dimension in [1,L] to be used as the target dimension of the \mathtt{fit} . More details below.	
	Passed internally to smooth.spline.	

Value

The backtransformed NxK (or NxD) matrix.

Target dimension

By default, the backtransform is such that afterward the signals are approximately proportional to the (first) principal curve as fitted by *fitPrincipalCurve(). This scale and origin of this principal curve is not uniquely defined. If targetDimension is specified, then the backtransformed signals are approximately proportional to the signals of the target dimension, and the signals in the target dimension are unchanged.

Subsetting dimensions

Argument dimensions can be used to backtransform a subset of dimensions (K) based on a subset of the fitted dimensions (L). If K=L, then both X and fit is subsetted. If K<>L, then it is assumed that X is already subsetted/expanded and only fit is subsetted.

See Also

```
*fitPrincipalCurve()
```

```
# Consider the case where K=4 measurements have been done # for the same underlying signals 'x'. The different measurements # have different systematic variation # y_k = f(x_k) + eps_k; k = 1, ..., K. # In this example, we assume non-linear measurement functions # f(x) = a + b * x + x * c + eps(b * x) # where 'a' is an offset, 'b' a scale factor, and 'c' an exponential. # We also assume heteroscedastic zero-mean noise with standard
```

```
# deviation proportional to the rescaled underlying signal 'x'.
\# Furthermore, we assume that measurements k=2 and k=3 undergo the
# same transformation, which may illustrate that the come from
# the same batch. However, when *fitting* the model below we
# will assume they are independent.
# Transforms
a < -c(2, 15, 15,
                 3)
b \leftarrow c(2, 3, 3, 4)
c \leftarrow c(1, 2, 2, 1/2)
K <- length(a)</pre>
# The true signal
N <- 1000
x <- rexp(N)
# The noise
bX <- outer(b,x)
E \leftarrow apply(bX, MARGIN=2, FUN=function(x) rnorm(K, mean=0, sd=0.1*x))
# The transformed signals with noise
Xc <- t(sapply(c, FUN=function(c) x^c))</pre>
Y \leftarrow a + bX + Xc + E
Y \leftarrow t(Y)
# Fit principal curve
# Fit principal curve through Y = (y_1, y_2, ..., y_K)
fit <- fitPrincipalCurve(Y)</pre>
# Flip direction of 'lambda'?
rho <- cor(fit$lambda, Y[,1], use="complete.obs")</pre>
flip <- (rho < 0)
if (flip) {
 fit$lambda <- max(fit$lambda, na.rm=TRUE)-fit$lambda</pre>
}
L <- ncol(fit$s)
# Backtransform data according to model fit
# Backtransform toward the principal curve (the "common scale")
YN1 <- backtransformPrincipalCurve(Y, fit=fit)</pre>
stopifnot(ncol(YN1) == K)
# Backtransform toward the first dimension
YN2 <- backtransformPrincipalCurve(Y, fit=fit, targetDimension=1)
stopifnot(ncol(YN2) == K)
# Backtransform toward the last (fitted) dimension
YN3 <- backtransformPrincipalCurve(Y, fit=fit, targetDimension=L)
stopifnot(ncol(YN3) == K)
```

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```
# Backtransform toward the third dimension (dimension by dimension)
\# Note, this assumes that K == L.
YN4 <- Y
for (cc in 1:L) {
  YN4[,cc] <- backtransformPrincipalCurve(Y, fit=fit,
                                  targetDimension=1, dimensions=cc)
stopifnot(identical(YN4, YN2))
# Backtransform a subset toward the first dimension
\# Note, this assumes that K == L.
YN5 <- backtransformPrincipalCurve(Y, fit=fit,
                               targetDimension=1, dimensions=2:3)
stopifnot(identical(YN5, YN2[,2:3]))
stopifnot(ncol(YN5) == 2)
# Extract signals from measurement #2 and backtransform according
# its model fit. Signals are standardized to target dimension 1.
y6 <- Y[,2,drop=FALSE]
yN6 <- backtransformPrincipalCurve(y6, fit=fit, dimensions=2,
                                               targetDimension=1)
stopifnot(identical(yN6, YN2[,2,drop=FALSE]))
stopifnot(ncol(yN6) == 1)
# Extract signals from measurement #2 and backtransform according
# the the model fit of measurement #3 (because we believe these
# two have undergone very similar transformations.
# Signals are standardized to target dimension 1.
y7 <- Y[,2,drop=FALSE]
yN7 <- backtransformPrincipalCurve(y7, fit=fit, dimensions=3,
                                               targetDimension=1)
stopifnot(ncol(yN7) == 1)
stopifnot(cor(yN7, yN6) > 0.9999)
```

calibrateMultiscan.matrix

Weighted affine calibration of a multiple re-scanned channel

Description

Weighted affine calibration of a multiple re-scanned channel.

Usage

```
## S3 method for class 'matrix':
calibrateMultiscan(X, weights=NULL, typeOfWeights=c("datapoint"), method="L1", c
```

Arguments

An NxK matrix (K>=2) where the columns represent the multiple scans of one channel (a two-color array contains two channels) to be calibrated.

Weights

If NULL, non-weighted normalization is done. If data-point weights are used,

If NULL, non-weighted normalization is done. If data-point weights are used, this should be a vector of length N of data point weights used when estimating the normalization function.

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typeOfWeights		
	$A \verb character string specifying the type of weights given in argument \verb weights .$	
method	A character string specifying how the estimates are robustified. See iwpca() for all accepted values.	
constraint	Constraint making the bias parameters identifiable. See $*fitIWPCA()$ for more details.	
satSignal	Signals equal to or above this threshold is considered saturated signals.	
	Other arguments passed to *fitIWPCA() and in turn iwpca().	
average	A function to calculate the average signals between calibrated scans.	
deviance	A function to calculate the deviance of the signals between calibrated scans.	
project	If TRUE, the calibrated data points projected onto the diagonal line, otherwise not. Moreover, if TRUE, argument average is ignored.	
.fitOnly	If TRUE, the data will not be back-transform.	

Details

Fitting is done by iterated re-weighted principal component analysis (IWPCA).

Value

If average is specified or project is TRUE, an Nx1 matrix is returned, otherwise an NxK matrix is returned. If deviance is specified, a deviance Nx1 matrix is returned as attribute deviance. In addition, the fitted model is returned as attribute modelFit.

Negative, non-positive, and saturated values

Affine multiscan calibration applies also to negative values, which are therefor also calibrated, if they exist.

Saturated signals in any scan are set to NA. Thus, they will not be used to estimate the calibration function, nor will they affect an optional projection.

Missing values

Only observations (rows) in X that contain all finite values are used in the estimation of the alibration functions. Thus, observations can be excluded by setting them to NA.

Weighted normalization

Each data point/observation, that is, each row in X, which is a vector of length K, can be assigned a weight in [0,1] specifying how much it should *affect the fitting of the calibration function*. Weights are given by argument weights, which should be a numeric vector of length N. Regardless of weights, all data points are *calibrated* based on the fitted calibration function.

Robustness

By default, the model fit of multiscan calibration is done in L_1 (method="L1"). This way, outliers affect the parameter estimates less than ordinary least-square methods.

When calculating the average calibrated signal from multiple scans, by default the median is used, which further robustify against outliers.

For further robustness, downweight outliers such as saturated signals, if possible.

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Tukey's biweight function is supported, but not used by default because then a "bandwidth" parameter has to selected. This can indeed be done automatically by estimating the standard deviation, for instance using MAD. However, since scanner signals have heteroscedastic noise (standard deviation is approximately proportional to the non-logged signal), Tukey's bandwidth parameter has to be a function of the signal too, cf. loess. We have experimented with this too, but found that it does not significantly improve the robustness compared to L_1 . Moreover, using Tukey's biweight as is, that is, assuming homoscedastic noise, seems to introduce a (scale dependent) bias in the estimates of the offset terms.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

[1] H. Bengtsson, J. Vallon-Christersson and G. Jönsson, *Calibration and assessment of channel-specific biases in microarray data with extended dynamical range*, BMC Bioinformatics, 5:177, 2004.

See Also

```
*normalizeAffine(). For more information see matrix.
```

Examples

```
## Not run: # For an example, see help(normalizeAffine).
```

distanceBetweenLines

Finds the shortest distance between two lines

Description

Finds the shortest distance between two lines.

Consider the two lines

```
x(s) = a_x + b_x * s \text{ and } y(t) = a_y + b_y * t
```

in an K-space where the offset and direction vectors are a_x and b_x (in R^K) that define the line x(s) (s is a scalar). Similar for the line y(t). This function finds the point (s,t) for which |x(s)-x(t)| is minimal.

Usage

```
## Default S3 method:
distanceBetweenLines(ax, bx, ay, by, ...)
```

Arguments

```
ax, bx Offset and direction vector of length K for line z_x. ay, by Offset and direction vector of length K for line z_y. Not used.
```

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Value

```
Returns the a list containing
```

```
ax, bx The given line x(s).

ay, by The given line y(t).

s,t The values of s and t such that |x(s)-y(t)| is minimal.

xs, yt The values of x(s) and y(t) at the optimal point (s,t).

distance The distance between the lines, i.e. |x(s)-y(t)| at the optimal point (s,t).
```

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

- [1] M. Bard and D. Himel, *The Minimum Distance Between Two Lines in n-Space*, September 2001, Advisor Dennis Merino.
- [2] Dan Sunday, Distance between Lines and Segments with their Closest Point of Approach, http://geometryalgorithms.com/Archive/algorithm_0106/.

```
for (zzz in 0) {
# This example requires plot3d() in R.basic [http://www.braju.com/R/]
if (!require(R.basic)) break
layout (matrix(1:4, nrow=2, ncol=2, byrow=TRUE))
************************
# Lines in two-dimensions
************************
x \leftarrow list(a=c(1,0), b=c(1,2))
y <- list(a=c(0,2), b=c(1,1))
fit <- distanceBetweenLines(ax=x$a, bx=x$b, ay=y$a, by=y$b)
xlim \leftarrow ylim \leftarrow c(-1,8)
plot(NA, xlab="", ylab="", xlim=ylim, ylim=ylim)
# Highlight the offset coordinates for both lines
points(t(x$a), pch="+", col="red")
text(t(x\$a), label=expression(a[x]), adj=c(-1,0.5))
points(t(y$a), pch="+", col="blue")
text(t(y$a), label=expression(a[y]), adj=c(-1,0.5))
v \leftarrow c(-1,1)*10;
xv \leftarrow list(x=x$a[1]+x$b[1]*v, y=x$a[2]+x$b[2]*v)
yv \leftarrow list(x=y$a[1]+y$b[1]*v, y=y$a[2]+y$b[2]*v)
lines(xv, col="red")
lines(yv, col="blue")
points(t(fit$xs), cex=2.0, col="red")
```

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```
text(t(fit$xs), label=expression(x(s)), adj=c(+2,0.5))
points(t(fit$yt), cex=1.5, col="blue")
text(t(fit\$yt), label=expression(y(t)), adj=c(-1,0.5))
print(fit)
# Lines in three-dimensions
x \leftarrow list(a=c(0,0,0), b=c(1,1,1)) # The 'diagonal'
y \leftarrow list(a=c(2,1,2), b=c(2,1,3)) # A 'fitted' line
fit <- distanceBetweenLines(ax=x$a, bx=x$b, ay=y$a, by=y$b)
xlim \leftarrow ylim \leftarrow zlim \leftarrow c(-1,3)
dummy <- t(c(1,1,1))*100;
# Coordinates for the lines in 3d
v < - seq(-10, 10, by=1);
xv \leftarrow list(x=x$a[1]+x$b[1]*v, y=x$a[2]+x$b[2]*v, z=x$a[3]+x$b[3]*v)
yv \leftarrow list(x=y$a[1]+y$b[1]*v, y=y$a[2]+y$b[2]*v, z=y$a[3]+y$b[3]*v)
for (theta in seq(30,140,length=3)) {
 plot3d(dummy, theta=theta, phi=30, xlab="", ylab="", zlab="",
                            xlim=ylim, ylim=ylim, zlim=zlim)
  # Highlight the offset coordinates for both lines
  points3d(t(x$a), pch="+", col="red")
  text3d(t(x$a), label=expression(a[x]), adj=c(-1,0.5))
  points3d(t(y$a), pch="+", col="blue")
  text3d(t(y$a), label=expression(a[y]), adj=c(-1,0.5))
  # Draw the lines
  lines3d(xv, col="red")
  lines3d(yv, col="blue")
  # Draw the two points that are closest to each other
  points3d(t(fit$xs), cex=2.0, col="red")
  text3d(t(fit$xs), label=expression(x(s)), adj=c(+2,0.5))
  points3d(t(fit$yt), cex=1.5, col="blue")
 text3d(t(fit$yt), label=expression(y(t)), adj=c(-1,0.5))
  # Draw the distance between the two points
  lines3d(rbind(fit$xs,fit$yt), col="purple", lwd=2)
print(fit)
} # for (zzz in 0)
rm(zzz)
```

fitIWPCA.matrix Robust fit of linear subspace through multidimensional data

Description

Robust fit of linear subspace through multidimensional data.

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Usage

```
## S3 method for class 'matrix':
fitIWPCA(X, constraint=c("diagonal", "baseline", "max"), baselineChannel=NULL,
```

Arguments

Χ

NxK matrix where N is the number of observations and K is the number of dimensions (channels).

constraint

A character string or a numeric value. If character it specifies which additional contraint to be used to specify the offset parameters along the fitted line:

If "diagonal", the offset vector will be a point on the line that is closest to the diagonal line (1,...,1). With this constraint, all bias parameters are identifiable.

If "baseline" (requires argument baselineChannel), the estimates are such that of the bias and scale parameters of the baseline channel is 0 and 1, respectively. With this constraint, all bias parameters are identifiable.

If "max", the offset vector will the point on the line that is as "great" as possible, but still such that each of its components is less than the corresponding minimal signal. This will guarantee that no negative signals are created in the backward transformation. If numeric value, the offset vector will the point on the line such that after applying the backward transformation there are constraint*N. Note that constraint==0 corresponds approximately to constraint=="max". With the latter two constraints, the bias parameters are only identifiable modulo the fitted line.

baselineChannel

Index of channel toward which all other channels are conform. This argument is required if constraint=="baseline". This argument is optional if constraint=="diagonal" and then the scale factor of the baseline channel will be one. The estimate of the bias parameters is not affected in this case. Defaults to one, if missing.

Additional arguments accepted by iwpca(). For instance, a N vector of weights for each observation may be given, otherwise they get the same weight.

aShift, Xmin For internal use only.

Details

This method uses re-weighted principal component analysis (IWPCA) to fit a the nodel $y_n = a + bx_n + eps_n$ where y_n , a, b, and eps_n are vector of the K and x_n is a scalar.

The algorithm is: For iteration i: 1) Fit a line L through the data close using weighted PCA with weights $\{w_n\}$. Let $r_n = \{r_{n,1},...,r_{n,K}\}$ be the K principal components. 2) Update the weights as $w_n < -1/\sum_{k=0}^{K} (r_{n,k} + \epsilon_r)$ where we have used the residuals of all but the first principal component. 3) Find the point a on L that is closest to the line D = (1,1,...,1). Similarly, denote the point on L that is closest to L by L and L that is closest to L by L and L the point of L that is closest to L by L and L that L that is closest to L by L and L that L that

Value

Returns a list that contains estimated parameters and algorithm details;

a A double vector (a[1], ..., a[K]) with offset parameter estimates. It is made identifiable according to argument constraint.

b	A double vector $(b[1],,b[K])$ with scale parameter estimates. It is made identifiable by constraining b [baselineChannel] == 1. These estimates are idependent of argument constraint.
adiag	If identifiability constraint "diagonal", a double vector $(adiag[1],,adiag[K])$, where $adiag[1] = adiag[2] =adiag[K]$, specifying the point on the diagonal line that is closest to the fitted line, otherwise the zero vector.
eigen	A KxK matrix with columns of eigenvectors.
converged	TRUE if the algorithm converged, otherwise FALSE.
nbr0fIterati	ons
	The number of iterations for the algorithm to converge, or zero if it did not converge.
	The second secon
t0	Internal parameter estimates, which contains no more information than the above listed elements.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

See Also

This is an internal method used by the \star fitMultiscanAffine() method, which in addition uses \star fitPairIWPCA(). Internally the function iwpca() is used to fit a line through the data cloud and the function distanceBetweenLines() to find the closest point to the diagonal (1,1,...,1).

```
fitPrincipalCurve.matrix
```

Fit a principal curve in K dimensions

Description

Fit a principal curve in K dimensions.

Usage

```
## S3 method for class 'matrix':
fitPrincipalCurve(X, ..., verbose=FALSE)
```

Arguments

```
X An NxK matrix (K>=2) where the columns represent the dimension.... Other arguments passed to principal.curve.verboseSee Verbose.
```

Value

Returns a principal.curve object (which is a list). See principal.curve for more details.

Missing values

The estimation of the affine normalization function will only be made based on complete observations, i.e. observations that contains no NA values in any of the channels.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

[1] Hastie, T. and Stuetzle, W, Principal Curves, JASA, 1989.

See Also

*backtransformPrincipalCurve().principal.curve.

```
\# Simulate data from the model y <- a + bx + x^c + eps(bx)
x < - rexp(1000)
a < -c(2, 15, 3)
b < -c(2,3,4)
c < -c(1,2,1/2)
bx <- outer(b,x)</pre>
xc <- t(sapply(c, FUN=function(c) x^c))</pre>
eps <- apply(bx, MARGIN=2, FUN=function(x) rnorm(length(x), mean=0, sd=0.1*x))
y \leftarrow a + bx + xc + eps
y <- t(y)
# Fit principal curve through (y_1, y_2, y_3)
fit <- fitPrincipalCurve(y)</pre>
# Flip direction of 'lambda'?
rho <- cor(fit$lambda, y[,1], use="complete.obs")</pre>
flip <- (rho < 0)
if (flip) {
  fit$lambda <- max(fit$lambda, na.rm=TRUE)-fit$lambda</pre>
}
\# Backtransform (y_1, y_2, y_3) to be proportional to each other
yN <- backtransformPrincipalCurve(y, fit=fit)</pre>
xlim <- c(0, 1.04*max(x))
ylim <- range(c(y,yN), na.rm=TRUE)</pre>
# Display raw and backtransform data
layout(matrix(1:4, nrow=2, byrow=TRUE))
par(mar=c(4,4,2,1)+0.1)
for (rr in 1:2) {
  ylab <- substitute(y[c], list=list(c=rr))</pre>
  for (cc in 2:3) {
    if (cc == rr) {
      plot.new()
      next
    }
```

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```
xlab <- substitute(y[c], list=list(c=cc))
plot(NA, xlim=ylim, ylim=ylim, xlab=xlab, ylab=ylab)
abline(a=0, b=1, lty=2)
points(y[,c(cc,rr)])
points(yN[,c(cc,rr)], col="tomato")
}

layout(matrix(1:4, nrow=2, byrow=TRUE))
par(mar=c(4,4,2,1)+0.1)
for (cc in 1:3) {
  ylab <- substitute(y[c], list=list(c=cc))
  plot(NA, xlim=xlim, ylim=ylim, xlab="x", ylab=ylab)
  points(x, y[,cc])
  points(x, yN[,cc], col="tomato")
}</pre>
```

iwpca.matrix

Fits an R-dimensional hyperplane using iterative re-weighted PCA

Description

Fits an R-dimensional hyperplane using iterative re-weighted PCA.

Usage

```
## S3 method for class 'matrix':
iwpca(X, w=NULL, R=1, method=c("symmetric", "bisquare", "tricube", "L1"), maxIte
```

Arguments

X	N-times-Kmatrix where N is the number of observations and K is the number of dimensions.
W	An N vector of weights for each row (observation) in the data matrix. If \mathtt{NULL} , all observations get the same weight.
R	Number of principal components to fit. By default a line is fitted.
method	If "symmetric" (or "bisquare"), Tukey's biweight is used. If "tricube", the tricube weight is used. If "L1", the model is fitted in L_1 . If a function, it is used to calculate weights for next iteration based on the current iteration's residuals.
maxIter	Maximum number of iterations.
acc	The (Euclidean) distance between two subsequent parameters fit for which the algorithm is considered to have converged.
reps	Small value to be added to the residuals before the the weights are calculated based on their inverse. This is to avoid infinite weights.
fit0	A list containing elements vt and pc specifying an initial fit. If NULL, the initial guess will be equal to the (weighted) PCA fit.
• • •	Additional arguments accepted by *wpca().

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Details

This method uses weighted principal component analysis (WPCA) to fit a R-dimensional hyperplane through the data with initial internal weights all equal. At each iteration the internal weights are recalculated based on the "residuals". If method=="L1", the internal weights are 1/sum(abs(r) + reps). This is the same as method=function(r) 1/sum(abs(r) + reps). The "residuals" are orthogonal Euclidean distance of the principal components R,R+1,...,K. In each iteration before doing WPCA, the internal weighted are multiplied by the weights given by argument w, if specified.

Value

Returns the fit (a list) from the last call to \star wpca() with the additional elements nbrOfIterations and converged.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

See Also

Internally *wpca() is used for calculating the weighted PCA.

```
for (zzz in 0) {
# This example requires plot3d() in R.basic [http://www.braju.com/R/]
if (!require(R.basic)) break
\# Simulate data from the model y <- a + bx + eps(bx)
x < - rexp(1000)
a < -c(2, 15, 3)
b < -c(2,3,4)
bx <- outer(b,x)</pre>
eps <- apply(bx, MARGIN=2, FUN=function(x) rnorm(length(x), mean=0, sd=0.1*x))
y \leftarrow a + bx + eps
y < -t(y)
\# Add some outliers by permuting the dimensions for 1/10 of the observations
idx <- sample(1:nrow(y), size=1/10*nrow(y))
y[idx,] \leftarrow y[idx,c(2,3,1)]
# Plot the data with fitted lines at four different view points
opar <- par (mar=c(1,1,1,1)+0.1)
N <- 4
layout(matrix(1:N, nrow=2, byrow=TRUE))
theta \leftarrow seq(0,270,length=N)
phi <- rep(20, length.out=N)
xlim <- ylim <- zlim <- c(0,45);
persp <- list();</pre>
for (kk in seq(theta)) {
  # Plot the data
  persp[[kk]] <- plot3d(y, theta=theta[kk], phi=phi[kk], xlim=xlim, ylim=ylim, zlim=zlim)</pre>
```

```
# Weights on the observations
# Example a: Equal weights
w <- NULL
# Example b: More weight on the outliers (uncomment to test)
w \leftarrow rep(1, length(x)); w[idx] \leftarrow 0.8
# ...and show all iterations too with different colors.
maxIter <- c(seq(1,20,length=10),Inf)</pre>
col <- topo.colors(length(maxIter))</pre>
# Show the fitted value for every iteration
for (ii in seg(along=maxIter)) {
  # Fit a line using IWPCA through data
  fit <- iwpca(y, w=w, maxIter=maxIter[ii], swapDirections=TRUE)
  ymid <- fit$xMean
  d0 <- apply(y, MARGIN=2, FUN=min) - ymid
  d1 <- apply(y, MARGIN=2, FUN=max) - ymid
  b <- fit$vt[1,]
  y0 < -b * max(abs(d0))
  y1 \leftarrow b * max(abs(d1))
  yline <- matrix(c(y0,y1), nrow=length(b), ncol=2)</pre>
  yline <- yline + ymid
  for (kk in seq(theta)) {
    # Set pane to draw in
    par(mfg=c((kk-1) %/% 2, (kk-1) %% 2) + 1);
    # Set the viewpoint of the pane
    options(persp.matrix=persp[[kk]]);
    # Get the first principal component
    points3d(t(ymid), col=col[ii])
    lines3d(t(yline), col=col[ii])
    # Highlight the last one
    if (ii == length(maxIter))
      lines3d(t(yline), col="red", lwd=3)
}
par(opar)
} # for (zzz in 0)
rm(zzz)
```

likelihood.smooth.spline

Calculate the log likelihood of a smoothing spline given the data

Description

Calculate the (log) likelihood of a spline given the data used to fit the spline, g. The likelihood consists of two main parts: 1) (weighted) residuals sum of squares, and 2) a penalty term. The penalty term consists of a *smoothing parameter lambda* and a *roughness measure* of the spline $J(g) = \int g''(t)dt$. Hence, the overall log likelihood is

$$\log L(g|x) = (y - g(x))'W(y - g(x)) + \lambda J(g)$$

In addition to the overall likelihood, all its seperate components are also returned.

Note: when fitting a smooth spline with (x,y) values where the x's are not unique, smooth.spline will replace such (x,y)'s with a new pair (x,y') where y' is a reweighted average on the original y's. It is important to be aware of this. In such cases, the resulting smooth.spline object does not contain all (x,y)'s and therefore this function will not calculate the weighted residuals sum of square on the original data set, but on the data set with unique x's. See examples below how to calculate the likelihood for the spline with the original data.

Usage

```
## S3 method for class 'smooth.spline':
likelihood(object, x=NULL, y=NULL, w=NULL, base=exp(1), rel.tol=.Machine$double.
```

Arguments

object	The smooth.spline object.
х, у	The x and y values for which the (weighted) likelihood will be calculated. If x is of type xy.coords any value of argument y will be omitted. If $x==NULL$, the x and y values of the smoothing spline will be used.
W	The weights for which the (weighted) likelihood will be calculated. If NULL, weights equal to one are assumed.
base	The base of the logarithm of the likelihood. If \mathtt{NULL} , the non-logged likelihood is returned.
rel.tol	The relative tolerance used in the call to integrate.
	Not used.

Details

The roughness penalty for the smoothing spline, g, fitted from data in the interval $\left[a,b\right]$ is defined as

 $J(g) = \int_{a}^{b} g''(t)dt$

which is the same as

$$J(g) = g'(b) - g'(a)$$

The latter is calculated internally by using predict.smooth.spline.

Value

Returns the overall (log) likelihood of class SmoothSplineLikelihood, a class with the following attributes:

wrss the (weighted) residual sum of square

penalty the penalty which is equal to -lambda*roughness.

lambda the smoothing parameter

roughness the value of the roughness functional given the specific smoothing spline and

the range of data

Author(s)

Henrik Bengtsson (http://www.braju.com/R/)

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See Also

```
smooth.spline and robustSmoothSpline().
```

Examples

```
# Define f(x)
f \leftarrow expression(0.1*x^4 + 1*x^3 + 2*x^2 + x + 10*sin(2*x))
# Simulate data from this function in the range [a,b]
a < -2; b < -5
x \leftarrow seq(a, b, length=3000)
y <- eval(f)
# Add some noise to the data
y \leftarrow y + rnorm(length(y), 0, 10)
# Plot the function and its second derivative
plot(x,y, type="1", lwd=4)
# Fit a cubic smoothing spline and plot it
g \leftarrow smooth.spline(x,y, df=16)
lines(g, col="yellow", lwd=2, lty=2)
# Calculating the (log) likelihood of the fitted spline
1 <- likelihood(g)</pre>
cat("Log likelihood with unique x values:\n")
print(1)
# Note that this is not the same as the log likelihood of the
\# data on the fitted spline iff the x values are non-unique
x[1:5] \leftarrow x[1] + Non-unique x values
g \leftarrow smooth.spline(x,y, df=16)
l <- likelihood(g)</pre>
cat("\nLog likelihood of the *spline* data set:\n");
print(1)
# In cases with non unique x values one has to proceed as
# below if one want to get the log likelihood for the original
1 <- likelihood(g, x=x, y=y)</pre>
cat("\nLog likelihood of the *original* data set:\n");
print(1)
```

medianPolish.matrix

Median polish

Description

Median polish.

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Usage

```
## S3 method for class 'matrix':
medianPolish(X, tol=0.01, maxIter=10, na.rm=NA, ..., .addExtra=TRUE)
```

Arguments

X	N-times-K matrix
tol	A numeric value greater than zero used as a threshold to identify when the algorithm has converged.
maxIter	Maximum number of iterations.
na.rm	If TRUE (FALSE), NAs are exclude (not exclude). If NA, it is assumed that $\tt X$ contains no NA values.
.addExtra	If TRUE, the name of argument X is returned and the returned structure is assigned a class. This will make the result compatible what $medpolish$ returns.
	Not used.

Details

The implementation of this method give identical estimates as medpolish, but is about 3-5 times more efficient when there are no NA values.

Value

Returns a named list structure with elements:

```
overall The fitted constant term.

row The fitted row effect.

col The fitted column effect.
```

residuals The residuals.

converged If TRUE, the algorithm converged, otherwise not.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

See Also

```
medpolish.
```

```
# Deaths from sport parachuting; from ABC of EDA, p.224:
deaths <- matrix(c(14,15,14, 7,4,7, 8,2,10, 15,9,10, 0,2,0), ncol=3, byrow=TRUE)
rownames(deaths) <- c("1-24", "25-74", "75-199", "200++", "NA")
colnames(deaths) <- 1973:1975

print(deaths)

mp <- medianPolish(deaths)
mp1 <- medpolish(deaths, trace=FALSE)
print(mp)</pre>
```

```
ff <- c("overall", "row", "col", "residuals")
stopifnot(all.equal(mp[ff], mp1[ff]))

# Validate decomposition:
stopifnot(all.equal(deaths, mp$overall+outer(mp$row,mp$col,"+")+mp$resid))</pre>
```

Non-documented objects

Non-documented objects

Description

This page contains aliases for all "non-documented" objects that R CMD check detects in this package.

Almost all of them are *generic* functions that have specific document for the corresponding method coupled to a specific class. Other functions are re-defined by setMethodS3() to *default* methods. Neither of these two classes are non-documented in reality. The rest are deprecated methods.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

```
normalizeAffine.matrix
```

Weighted affine normalization between channels and arrays

Description

Weighted affine normalization between channels and arrays.

This method will both remove curvature in the M vs A plots that are due to an affine transformation of the data. In other words, if there are (small or large) biases in the different (red or green) channels, biases that can be equal too, you will get curvature in the M vs A plots and this type of curvature will be removed by this normalization method.

Moreover, if you normalize all slides at once, this method will also bring the signals on the same scale such that the log-ratios for different slides are comparable. Thus, do not normalize the scale of the log-ratios between slides afterward.

It is recommended to normalize as many slides as possible in one run. The result is that if creating log-ratios between any channels and any slides, they will contain as little curvature as possible.

Furthermore, since the relative scale between any two channels on any two slides will be one if one normalizes all slides (and channels) at once it is possible to add or multiply with the *same* constant to all channels/arrays without introducing curvature. Thus, it is easy to rescale the data afterwards as demonstrated in the example.

Usage

```
## S3 method for class 'matrix':
normalizeAffine(X, weights=NULL, typeOfWeights=c("datapoint"), method="L1", cons
```

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Arguments

	X	An NxK \mathtt{matrix} (K>=2) where the columns represent the channels, to be normalized.
	weights	If NULL, non-weighted normalization is done. If data-point weights are used, this should be a vector of length N of data point weights used when estimating the normalization function.
typeOfWeights		
		$A \verb character string specifying the type of weights given in argument \verb weights .$
	method	A character string specifying how the estimates are robustified. See $iwpca()$ for all accepted values.
	constraint	Constraint making the bias parameters identifiable. See $\star \texttt{fitIWPCA}$ () for more details.
	satSignal	Signals equal to or above this threshold will not be used in the fitting.
	•••	Other arguments passed to *fitIWPCA() and in turn iwpca(). For example, the weight argument of iwpca(). See also below.
	.fitOnly	If TRUE, the data will not be back-transform.

Details

A line is fitted robustly throught the (y_R, y_G) observations using an iterated re-weighted principal component analysis (IWPCA), which minimized the residuals that are orthogonal to the fitted line. Each observation is down-weighted by the inverse of the absolute residuals, i.e. the fit is done in L_1 .

Value

A NxK matrix of the normalized channels. The fitted model is returned as attribute modelFit.

Negative, non-positive, and saturated values

Affine normalization applies equally well to negative values. Thus, contrary to normalization methods applied to log-ratios, such as curve-fit normalization methods, affine normalization, will not set these to NA.

Data points that are saturated in one or more channels are not used to estimate the normalization function, but they are normalized.

Missing values

The estimation of the affine normalization function will only be made based on complete non-saturated observations, i.e. observations that contains no NA values nor saturated values as defined by satSignal.

Weighted normalization

Each data point/observation, that is, each row in X, which is a vector of length K, can be assigned a weight in [0,1] specifying how much it should affect the fitting of the affine normalization function. Weights are given by argument weights, which should be a numeric vector of length N. Regardless of weights, all data points are normalized based on the fitted normalization function.

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Robustness

By default, the model fit of affine normalization is done in L_1 (method="L1"). This way, outliers affect the parameter estimates less than ordinary least-square methods.

For further robustness, downweight outliers such as saturated signals, if possible.

We do not use Tukey's biweight function for reasons similar to those outlined in *calibrateMultiscan().

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

[1] Henrik Bengtsson and Ola Hössjer, *Methodological Study of Affine Transformations of Gene Expression Data*, Methodological study of affine transformations of gene expression data with proposed robust non-parametric multi-dimensional normalization method, BMC Bioinformatics, 2006, 7:100.

See Also

```
*calibrateMultiscan().
```

```
pathname <- system.file("data-ex", "PMT-RGData.dat", package="aroma.light")</pre>
rg <- read.table(pathname, header=TRUE, sep="\t")</pre>
nbrOfScans <- max(rg$slide)</pre>
rg <- as.list(rg)
for (field in c("R", "G"))
 rg[[field]] <- matrix(as.double(rg[[field]]), ncol=nbrOfScans)</pre>
rg$slide <- rg$spot <- NULL
rg <- as.matrix(as.data.frame(rg))</pre>
colnames(rg) <- rep(c("R", "G"), each=nbrOfScans)</pre>
layout (matrix(c(1,2,0,3,4,0,5,6,7), ncol=3, byrow=TRUE))
rgC <- rg
for (channel in c("R", "G")) {
 sidx <- which(colnames(rg) == channel)</pre>
 channelColor <- switch(channel, R="red", G="green");</pre>
  # The raw data
  plotMvsAPairs(rg[,sidx])
 title(main=paste("Observed", channel))
 box(col=channelColor)
  # The calibrated data
 rgC[,sidx] <- calibrateMultiscan(rg[,sidx], average=NULL)</pre>
 plotMvsAPairs(rgC[,sidx])
```

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```
title(main=paste("Calibrated", channel))
 box(col=channelColor)
} # for (channel ...)
# The average calibrated data
# Note how the red signals are weaker than the green. The reason
# for this can be that the scale factor in the green channel is
# greater than in the red channel, but it can also be that there
# is a remaining relative difference in bias between the green
# and the red channel, a bias that precedes the scanning.
rqCA <- rq
for (channel in c("R", "G")) {
 sidx <- which(colnames(rg) == channel)</pre>
 rgCA[,sidx] <- calibrateMultiscan(rg[,sidx])</pre>
}
rgCAavg <- matrix(NA, nrow=nrow(rgCA), ncol=2)
colnames(rgCAavg) <- c("R", "G");</pre>
for (channel in c("R", "G")) {
 sidx <- which(colnames(rg) == channel)</pre>
 rgCAavg[,channel] <- apply(rgCA[,sidx], MARGIN=1, FUN=median, na.rm=TRUE);
# Add some "fake" outliers
outliers <- 1:600
rgCAavg[outliers, "G"] <- 50000;
plotMvsA(rgCAavg)
title(main="Average calibrated (AC)")
# Normalize data
# Weight-down outliers when normalizing
weights <- rep(1, nrow(rgCAavg));</pre>
weights[outliers] <- 0.001;</pre>
# Affine normalization of channels
rgCANa <- normalizeAffine(rgCAavg, weights=weights)</pre>
# It is always ok to rescale the affine normalized data if its
\# done on (R,G); not on (A,M)! However, this is only needed for
# esthetic purposes.
rgCANa <- rgCANa *2^1.4
plotMvsA(rgCANa)
title(main="Normalized AC")
# Curve-fit (lowess) normalization
rgCANlw <- normalizeLowess(rgCAavg, weights=weights)
plotMvsA(rgCANlw, col="orange", add=TRUE)
# Curve-fit (loess) normalization
rgCANl <- normalizeLoess(rgCAavg, weights=weights)</pre>
plotMvsA(rgCAN1, col="red", add=TRUE)
```

normalizeAverage.matrix

Rescales channel vectors to get the same average

Description

Rescales channel vectors to get the same average.

Usage

```
## S3 method for class 'matrix':
normalizeAverage(x, baseline=1, avg=median, targetAvg=2200, ...)
```

Arguments

A numeric NxK matrix (or list of length K).

An integer in [1,K] specifying which channel should be the baseline.

A function for calculating the average of one channel.

The average that each channel should have afterwards. If NULL, the baseline column sets the target average.

Additional arguments passed to the avg function.

Value

Returns a normalized numeric NxK matrix (or list of length K).

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

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```
normalizeCurveFit.matrix
```

Weighted curve-fit normalization between a pair of channels

Description

Weighted curve-fit normalization between a pair of channels.

This method will estimate a smooth function of the dependency between the log-ratios and the log-intensity of the two channels and then correct the log-ratios (only) in order to remove the dependency. This is method is also known as *intensity-dependent* or *lowess normalization*.

The curve-fit methods are by nature limited to paired-channel data. There exist at least one method trying to overcome this limitation, namely the cyclic-lowess [1], which applies the paired curve-fit method iteratively over all pairs of channels/arrays. Cyclic-lowess is not implented here.

We recommend that affine normalization [2] is used instead of curve-fit normalization.

Usage

```
## S3 method for class 'matrix':
normalizeCurveFit(X, weights=NULL, typeOfWeights=c("datapoint"), method=c("loess")
```

Arguments

X An Nx2 matrix where the columns represent the two channels to be normal-

ized.

weights If NULL, non-weighted normalization is done. If data-point weights are used,

this should be a $\ensuremath{\text{vector}}$ of length N of data point weights used when estimating

the normalization function.

typeOfWeights

A character string specifying the type of weights given in argument weights.

method character string specifying which method to use when fitting the intensity-

dependent function. Supported methods: "loess" (better than lowess), "lowess" (classic; supports only zero-one weights), "spline" (more robust than lowess at lower and upper intensities; supports only zero-one weights), "robustSpline"

(better than spline).

 $\label{eq:bandwidth} \text{A double value specifying the bandwidth of the estimator used.}$

satSignal Signals equal to or above this threshold will not be used in the fitting.

... Not used.

Details

A smooth function c(A) is fitted throught data in (A, M), where $M = log_2(y_2/y_1)$ and $A = 1/2 * log_2(y_2 * y_1)$. Data is normalized by M < -M - c(A).

Loess is by far the slowest method of the four, then lowess, and then robust spline, which iteratively calls the spline method.

Value

A Nx2 matrix of the normalized two channels. The fitted model is returned as attribute modelFit.

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Negative, non-positive, and saturated values

Non-positive values are set to not-a-number (NaN). Data points that are saturated in one or more channels are not used to estimate the normalization function, but they are normalized.

Missing values

The estimation of the affine normalization function will only be made based on complete non-saturated observations, i.e. observations that contains no NA values nor saturated values as defined by satSignal.

Weighted normalization

Each data point, that is, each row in X, which is a vector of length 2, can be assigned a weight in [0,1] specifying how much it should affect the fitting of the affine normalization function. Weights are given by argument weights, which should be a numeric vector of length N. Regardless of weights, all data points are normalized based on the fitted normalization function.

Note that the lowess and the spline method only support zero-one $\{0,1\}$ weights. For such methods, all weights that are less than a half are set to zero.

Details on loess

```
For loess, the arguments family="symmetric", degree=1, span=3/4, control=loess.control(traciterations=5, surface="direct") are used.
```

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

[1] M. Åstrand, Contrast Normalization of Oligonucleotide Arrays, Journal Computational Biology, 2003, 10, 95-102.

[2] Henrik Bengtsson and Ola Hössjer, *Methodological Study of Affine Transformations of Gene Expression Data*, Methodological study of affine transformations of gene expression data with proposed robust non-parametric multi-dimensional normalization method, BMC Bioinformatics, 2006, 7:100.

See Also

```
*normalizeAffine().
```

```
pathname <- system.file("data-ex", "PMT-RGData.dat", package="aroma.light")
rg <- read.table(pathname, header=TRUE, sep="\t")
nbrOfScans <- max(rg$slide)

rg <- as.list(rg)
for (field in c("R", "G"))
   rg[[field]] <- matrix(as.double(rg[[field]]), ncol=nbrOfScans)
rg$slide <- rg$spot <- NULL
rg <- as.matrix(as.data.frame(rg))
colnames(rg) <- rep(c("R", "G"), each=nbrOfScans)</pre>
```

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```
layout (matrix(c(1,2,0,3,4,0,5,6,7), ncol=3, byrow=TRUE))
rgC <- rg
for (channel in c("R", "G")) {
 sidx <- which(colnames(rg) == channel)</pre>
 channelColor <- switch(channel, R="red", G="green");</pre>
 # The raw data
 plotMvsAPairs(rg[,sidx])
 title(main=paste("Observed", channel))
 box(col=channelColor)
 # The calibrated data
 rgC[,sidx] <- calibrateMultiscan(rg[,sidx], average=NULL)</pre>
 plotMvsAPairs(rqC[,sidx])
 title(main=paste("Calibrated", channel))
 box(col=channelColor)
} # for (channel ...)
# The average calibrated data
# Note how the red signals are weaker than the green. The reason
# for this can be that the scale factor in the green channel is
# greater than in the red channel, but it can also be that there
# is a remaining relative difference in bias between the green
# and the red channel, a bias that precedes the scanning.
rgCA <- rg
for (channel in c("R", "G")) {
 sidx <- which(colnames(rg) == channel)</pre>
 rgCA[,sidx] <- calibrateMultiscan(rg[,sidx])</pre>
}
rgCAavg <- matrix(NA, nrow=nrow(rgCA), ncol=2)</pre>
colnames(rgCAavg) <- c("R", "G");</pre>
for (channel in c("R", "G")) {
 sidx <- which(colnames(rg) == channel)</pre>
 rgCAavg[,channel] <- apply(rgCA[,sidx], MARGIN=1, FUN=median, na.rm=TRUE);
# Add some "fake" outliers
outliers <- 1:600
rgCAavg[outliers, "G"] <- 50000;
plotMvsA(rgCAavg)
title (main="Average calibrated (AC)")
# Normalize data
```

```
# Weight-down outliers when normalizing
weights <- rep(1, nrow(rgCAavg));</pre>
weights[outliers] <- 0.001;</pre>
# Affine normalization of channels
rgCANa <- normalizeAffine(rgCAavg, weights=weights)
# It is always ok to rescale the affine normalized data if its
\# done on (R,G); not on (A,M)! However, this is only needed for
# esthetic purposes.
rgCANa <- rgCANa *2^1.4
plotMvsA(rqCANa)
title(main="Normalized AC")
# Curve-fit (lowess) normalization
rgCANlw <- normalizeLowess(rgCAavg, weights=weights)
plotMvsA(rgCANlw, col="orange", add=TRUE)
# Curve-fit (loess) normalization
rgCAN1 <- normalizeLoess(rgCAavg, weights=weights)
plotMvsA(rgCAN1, col="red", add=TRUE)
# Curve-fit (robust spline) normalization
rgCANrs <- normalizeRobustSpline(rgCAavg, weights=weights)
plotMvsA(rgCANrs, col="blue", add=TRUE)
legend(x=0,y=16, legend=c("affine", "lowess", "loess", "r. spline"), pch=19,
       col=c("black", "orange", "red", "blue"), ncol=2, x.intersp=0.3, bty="n")
plotMvsMPairs(cbind(rgCANa, rgCANlw), col="orange", xlab=expression(M[affine]))
title (main="Normalized AC")
plotMvsMPairs(cbind(rgCANa, rgCANl), col="red", add=TRUE)
plotMvsMPairs(cbind(rgCANa, rgCANrs), col="blue", add=TRUE)
abline (a=0, b=1, lty=2)
legend(x=-6,y=6, legend=c("lowess", "loess", "r. spline"), pch=19,
       col=c("orange", "red", "blue"), ncol=2, x.intersp=0.3, bty="n")
```

normalizeFragmentLength

Normalizes signals for PCR fragment-length effects

Description

Normalizes signals for PCR fragment-length effects. Some or all signals are used to estimated the normalization function. All signals are normalized.

Usage

```
## Default S3 method:
normalizeFragmentLength(y, fragmentLengths, targetFcns=NULL, subsetToFit=NULL, c
```

Arguments

A numeric vector of length K of signals to be normalized across E enzymes. fragmentLengths An integer KxE matrix of fragment lengths. An optional list of E functions; one per enzyme. If NULL, the data is targetFcns normalized to have constant fragment-length effects (all equal to zero on the log-scale). subsetToFit The subset of data points used to fit the normalization function. If NULL, all data points are considered. Specifies how data points for which there is no fragment length is normalized. If onMissing "ignore", the values are not modified. If "median", the values are updated to have the same robust average as the other data points. .isLogged A logical. Additional arguments passed to lowess. .returnFit A logical.

Value

Returns a numeric vector of the normalized signals.

Multi-enzyme normalization

It is assumed that the fragment-length effects from multiple enzymes added (with equal weights) on the intensity scale. The fragment-length effects are fitted for each enzyme separately based on units that are exclusively for that enzyme. If there are no or very such units for an enzyme, the assumptions of the model are not met and the fit will fail with an error. Then, from the above single-enzyme fits the average effect across enzymes is the calculated for each unit that is on multiple enzymes.

Target functions

It is possible to specify custom target function effects for each enzyme via argument targetFcns. This argument has to be a list containing one function per enzyme and ordered in the same order as the enzyme are in the columns of argument fragmentLengths. For instance, if one wish to normalize the signals such that their mean signal as a function of fragment length effect is contantly equal to 2200 (or the intensity scale), the use targetFcns=function(fl, ...) log2(2200) which completely ignores fragment-length argument 'fl' and always returns a constant. If two enzymes are used, then use targetFcns=rep(list(function(fl, ...) log2(2200)), 2).

```
Note, if targetFcns is NULL, this corresponds to targetFcns=rep(list(function(fl, ...) 0), ncol(fragmentLengths)).
```

Alternatively, if one wants to only apply minimial corrections to the signals, then one can normalize toward target functions that correspond to the fragment-length effect of the average array.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

[1] H. Bengtsson, R. Irizarry, B. Carvalho, and T. Speed, *Estimation and assessment of raw copy numbers at the single locus level*, Bioinformatics, 2008.

```
# Example 1: Single-enzyme fragment-length normalization of 6 arrays
# Number samples
I <- 9;
# Number of loci
J <- 1000;
# Fragment lengths
fl <- seq(from=100, to=1000, length.out=J);</pre>
# Simulate data points with unknown fragment lengths
hasUnknownFL <- seq(from=1, to=J, by=50);
fl[hasUnknownFL] <- NA;</pre>
# Simulate data
y <- matrix(0, nrow=J, ncol=I);
maxY <- 12;
for (kk in 1:I) {
 k <- runif(n=1, min=3, max=5);</pre>
 mu <- function(fl) {</pre>
   mu <- rep(maxY, length(fl));</pre>
   ok <- !is.na(fl);
   mu[ok] \leftarrow mu[ok] - fl[ok]^{1/k};
   mu;
 eps <- rnorm(J, mean=0, sd=1);</pre>
 y[,kk] \leftarrow mu(fl) + eps;
}
# Normalize data (to a zero baseline)
yN <- apply(y, MARGIN=2, FUN=function(y) {
 \verb|normalizeFragmentLength(y, fragmentLengths=fl, on \verb|Missing="median")|;
})
# The correction factors
rho <- y-yN;
print(summary(rho));
# The correction for units with unknown fragment lengths
# equals the median correction factor of all other units
print(summary(rho[hasUnknownFL,]));
# Plot raw data
layout (matrix(1:9, ncol=3));
xlim <- c(0, max(fl, na.rm=TRUE));</pre>
ylim <- c(0, max(y, na.rm=TRUE));</pre>
xlab <- "Fragment length";</pre>
ylab <- expression(log2(theta));</pre>
```

```
for (kk in 1:I) {
  plot(f1, y[,kk], xlim=xlim, ylim=ylim, xlab=xlab, ylab=ylab);
  ok <- (is.finite(fl) & is.finite(y[,kk]));</pre>
  lines(lowess(fl[ok], y[ok,kk]), col="red", lwd=2);
# Plot normalized data
layout (matrix(1:9, ncol=3));
ylim <-c(-1,1)*max(y, na.rm=TRUE)/2;
for (kk in 1:I) {
 plot(fl, yN[,kk], xlim=xlim, ylim=ylim, xlab=xlab, ylab=ylab);
 ok <- (is.finite(fl) & is.finite(y[,kk]));</pre>
  lines(lowess(fl[ok], yN[ok,kk]), col="blue", lwd=2);
   # Example 2: Two-enzyme fragment-length normalization of 6 arrays
set.seed(0xbeef);
# Number samples
I <- 5;
# Number of loci
J <- 3000;
# Fragment lengths (two enzymes)
fl <- matrix(0, nrow=J, ncol=2);</pre>
fl[,1] <- seq(from=100, to=1000, length.out=J);
fl[,2] <- seq(from=1000, to=100, length.out=J);
# Let 1/2 of the units be on both enzymes
fl[seq(from=1, to=J, by=4),1] \leftarrow NA;
fl[seq(from=2, to=J, by=4),2] \leftarrow NA;
# Let some have unknown fragment lengths
hasUnknownFL <- seq(from=1, to=J, by=15);
fl[hasUnknownFL,] <- NA;</pre>
# Sty/Nsp mixing proportions:
rho <- rep(1, I);
rho[1] \leftarrow 1/3; # Less Sty in 1st sample
rho[3] <- 3/2; # More Sty in 3rd sample
# Simulate data
z \leftarrow array(0, dim=c(J,2,I));
maxLog2Theta <- 12;</pre>
for (ii in 1:I) {
  # Common effect for both enzymes
 mu <- function(fl) {</pre>
   k \leftarrow runif(n=1, min=3, max=5);
   mu <- rep(maxLog2Theta, length(fl));</pre>
   ok <- is.finite(fl);</pre>
   mu[ok] \leftarrow mu[ok] - fl[ok]^{1/k};
    mu;
```

```
# Calculate the effect for each data point
  for (ee in 1:2) {
    z[,ee,ii] <- mu(fl[,ee]);</pre>
  # Update the Sty/Nsp mixing proportions
  ee <- 2;
  z[,ee,ii] \leftarrow rho[ii]*z[,ee,ii];
  # Add random errors
  for (ee in 1:2) {
    eps <- rnorm(J, mean=0, sd=1/sqrt(2));
    z[,ee,ii] \leftarrow z[,ee,ii] + eps;
  }
}
hasFl <- is.finite(fl);</pre>
unitSets <- list(
 nsp = which(hasFl[,1] & !hasFl[,2]),
 sty = which(!hasFl[,1] & hasFl[,2]),
 both = which( hasFl[,1] & hasFl[,2]),
 none = which(!hasFl[,1] & !hasFl[,2])
# The observed data is a mix of two enzymes
theta <- matrix(NA, nrow=J, ncol=I);</pre>
# Single-enzyme units
for (ee in 1:2) {
 uu <- unitSets[[ee]];</pre>
 theta[uu,] <- 2^z[uu,ee,];
# Both-enzyme units (sum on intensity scale)
uu <- unitSets$both;
theta[uu,] <- (2^z[uu,1,]+2^z[uu,2,])/2;
# Missing units (sample from the others)
uu <- unitSets$none;
theta[uu,] <- apply(theta, MARGIN=2, sample, size=length(uu))
# Calculate target array
thetaT <- rowMeans(theta, na.rm=TRUE);</pre>
targetFcns <- list();</pre>
for (ee in 1:2) {
 uu <- unitSets[[ee]];</pre>
 fit <- lowess(fl[uu,ee], log2(thetaT[uu]));</pre>
 class(fit) <- "lowess";</pre>
 targetFcns[[ee]] <- function(fl, ...) {</pre>
    predict(fit, newdata=fl);
 }
}
# Fit model only to a subset of the data
subsetToFit <- setdiff(1:J, seq(from=1, to=J, by=10))</pre>
```

```
# Normalize data (to a target baseline)
thetaN <- matrix(NA, nrow=J, ncol=I);
fits <- vector("list", I);</pre>
for (ii in 1:I) {
  lthetaNi <- normalizeFragmentLength(log2(theta[,ii]), targetFcns=targetFcns,</pre>
                      fragmentLengths=fl, onMissing="median",
                      subsetToFit=subsetToFit, .returnFit=TRUE);
  fits[[ii]] <- attr(lthetaNi, "modelFit");</pre>
  thetaN[,ii] <- 2^lthetaNi;
}
# Plot raw data
xlim <- c(0, max(fl, na.rm=TRUE));</pre>
ylim <- c(0, max(log2(theta), na.rm=TRUE));</pre>
Mlim <- c(-1,1) *4;
xlab <- "Fragment length";</pre>
ylab <- expression(log2(theta));</pre>
Mlab <- expression(M==log[2](theta/theta[R]));</pre>
layout(matrix(1:(3*I), ncol=I, byrow=TRUE));
for (ii in 1:I) {
  plot(NA, xlim=xlim, ylim=ylim, xlab=xlab, ylab=ylab, main="raw");
  # Single-enzyme units
  for (ee in 1:2) {
    # The raw data
    uu <- unitSets[[ee]];
    points(fl[uu,ee], log2(theta[uu,ii]), col=ee+1);
  # Both-enzyme units (use fragment-length for enzyme #1)
  uu <- unitSets$both;
  points(fl[uu,1], log2(theta[uu,ii]), col=3+1);
  for (ee in 1:2) {
    # The true effects
    uu <- unitSets[[ee]];
    lines(lowess(fl[uu,ee], log2(theta[uu,ii])), col="black", lwd=4, lty=3);
    # The estimated effects
    fit <- fits[[ii]][[ee]]$fit;</pre>
    lines(fit, col="orange", lwd=3);
    muT <- targetFcns[[ee]](fl[uu,ee]);</pre>
    lines(fl[uu,ee], muT, col="cyan", lwd=1);
}
# Calculate log-ratios
thetaR <- rowMeans(thetaN, na.rm=TRUE);</pre>
M <- log2(thetaN/thetaR);</pre>
# Plot normalized data
for (ii in 1:I) {
  plot(NA, xlim=xlim, ylim=Mlim, xlab=xlab, ylab=Mlab, main="normalized");
  # Single-enzyme units
  for (ee in 1:2) {
```

```
# The normalized data
    uu <- unitSets[[ee]];
    points(fl[uu,ee], M[uu,ii], col=ee+1);
  # Both-enzyme units (use fragment-length for enzyme #1)
  uu <- unitSets$both;
  points(fl[uu,1], M[uu,ii], col=3+1);
ylim <- c(0, 1.5);
for (ii in 1:I) {
  data <- list();</pre>
  for (ee in 1:2) {
    # The normalized data
   uu <- unitSets[[ee]];
    data[[ee]] <- M[uu,ii];</pre>
  uu <- unitSets$both;
  if (length(uu) > 0)
    data[[3]] <- M[uu,ii];</pre>
  uu <- unitSets$none;
  if (length(uu) > 0)
    data[[4]] <- M[uu,ii];</pre>
  cols <- seq(along=data)+1;</pre>
  plotDensity(data, col=cols, xlim=Mlim, xlab=Mlab, main="normalized");
  abline (v=0, lty=2);
```

normalizeQuantileRank.list

Normalizes the empirical distribution of a set of samples to a target distribution

Description

Normalizes the empirical distribution of a set of samples to a target distribution. The samples may differ in size.

Usage

```
## S3 method for class 'list':
normalizeQuantileRank(X, xTarget=NULL, ...)
```

Arguments

```
X a list with numeric vectors. The vectors may be of different lengths.

xTarget The target empirical distribution. If NULL, the target distribution is calculated as the average empirical distribution of the samples.
```

... Passed to normalizeQuantileRank.numeric().

Value

Returns a list of normalized numeric vector of the same lengths as the corresponding ones in the input matrix.

Missing values

Missing values are excluded. Values that are NA remain NA after normalization. No new NAs are introduced.

Author(s)

Adopted from Gordon Smyth (http://www.statsci.org/) in 2002 & 2006. Original code by Ben Bolstad at Statistics Department, University of California.

See Also

The target empirical distribution is calculated as the average using *averageQuantile(). Each vector is normalized toward this target disribution using *normalizeQuantileRank.numeric(). *normalizeQuantileSpline().

```
# Simulate ten samples of different lengths
N < -10000
X \leftarrow list()
for (kk in 1:8) {
  rfcn <- list(rnorm, rgamma)[[sample(2, size=1)]]</pre>
  size <- runif(1, min=0.3, max=1)</pre>
  a <- rgamma(1, shape=20, rate=10)</pre>
  b <- rgamma(1, shape=10, rate=10)</pre>
  values <- rfcn(size*N, a, b)</pre>
  # "Censor" values
  values[values < 0 | values > 8] <- NA
  X[[kk]] \leftarrow values
# Add 20% missing values
X <- lapply(X, FUN=function(x) {</pre>
  x[sample(length(x), size=0.20*length(x))] <- NA;
})
# Normalize quantiles
Xn <- normalizeQuantile(X)</pre>
# Plot the data
layout(matrix(1:2, ncol=1))
xlim <- range(X, na.rm=TRUE);</pre>
plotDensity(X, lwd=2, xlim=xlim, main="The original distributions")
plotDensity(Xn, lwd=2, xlim=xlim, main="The normalized distributions")
```

```
normalizeQuantileRank.matrix
```

Weighted sample quantile normalization

Description

Normalizes channels so they all have the same average sample distributions.

The average sample distribution is calculated either robustly or not by utilizing either weightedMedian() or weighted.mean(). A weighted method is used if any of the weights are different from one.

Usage

```
## S3 method for class 'matrix':
normalizeQuantileRank(X, ties=FALSE, robust=FALSE, weights=NULL, typeOfWeights=0
```

Arguments

X	a numerical NxK matrix with the K columns representing the channels and the N rows representing the data points.	
robust	If TRUE, the (weighted) median function is used for calculating the average sample distribution, otherwise the (weighted) mean function is used.	
ties	Should ties be specially treated or not?	
weights	If NULL, non-weighted normalization is done. If channel weights, this should be a vector of length K specifying the weights for each channel. If signal weights, it should be an NxK matrix specifying the weights for each signal.	
typeOfWeights		
	$A\hbox{\tt character}\hbox{\tt string}\hbox{\tt specifying}\hbox{\tt the}\hbox{\tt type}\hbox{\tt of}\hbox{\tt weights}\hbox{\tt given}\hbox{\tt in}\hbox{\tt argument}\hbox{\tt weights}.$	

... Not used.

Value

Returns an NxK matrix.

Missing values

Missing values are excluded when estimating the "common" (the baseline) distribution. Values that are NA before remain NA. No new NAs are introduced.

Weights

Currently only channel weights are support due to the way quantile normalization is done. If signal weights are given, channel weights are calculated from these by taking the mean of the signal weights in each channel.

Author(s)

Adopted from Gordon Smyth (http://www.statsci.org/) in 2002 & 2006. Original code by Ben Bolstad at Statistics Department, University of California. Support for calculating the average sample distribution using (weighted) mean or median was added by Henrik Bengtsson (http://www.braju.com/R/).

See Also

```
median, weightedMedian(), mean() and weighted.mean. *normalizeQuantileSpline().
```

Examples

normalizeQuantileRank.numeric

Normalizes the empirical distribution of a single sample to a target distribution

Description

Normalizes the empirical distribution of a single sample to a target distribution.

Usage

```
## S3 method for class 'numeric':
normalizeQuantileRank(x, xTarget, ties=FALSE, ...)
```

Arguments

Value

Returns a numeric vector of length N.

Missing values

It is only the empirical distribution of the non-missing values that is normalized to the target distribution. All NA values remain NA after normalization. No new NAs are introduced.

Author(s)

Adopted from Gordon Smyth (http://www.statsci.org/) in 2002 & 2006. Original code by Ben Bolstad at Statistics Department, University of California.

See Also

To calculate a target distribution from a set of samples, see *getAverageQuantile(). This method is used by normalizeQuantileRank.list(). *normalizeQuantileSpline().

```
normalizeQuantileSpline.list
```

Normalizes the empirical distribution of a set of samples to a target distribution

Description

Normalizes the empirical distribution of a set of samples to a target distribution. The samples may differ in size.

Usage

```
## S3 method for class 'list':
normalizeQuantileSpline(X, xTarget=NULL, ...)
```

Arguments

```
    X a list with numeric vectors. The vectors may be of different lengths.
    xTarget The target empirical distribution. If NULL, the target distribution is calculated as the average empirical distribution of the samples.
    ... Passed to normalizeQuantileSpline.numeric().
```

Value

Returns a list of normalized numeric vector of the same lengths as the corresponding ones in the input matrix.

Missing values

Missing values are excluded. Values that are NA remain NA after normalization. No new NAs are introduced.

Author(s)

Henrik Bengtsson, Statistics Department, University of California at Berkeley.

See Also

```
The target empirical distribution is calculated as the average using *averageQuantile(). Each vector is normalized toward this target disribution using *normalizeQuantileSpline.numeric(). *normalizeQuantileRank().
```

```
normalizeQuantileSpline.matrix
```

Weighted sample quantile normalization

Description

Normalizes channels so they all have the same average sample distributions.

Usage

```
## S3 method for class 'matrix':
normalizeQuantileSpline(X, xTarget, ...)
```

Arguments

X A numeric NxK matrix with the K columns representing the channels and the N rows representing the data points.
 xTarget A numeric vector of length N.
 ... Additional arguments passed to normalizeQuantileSpline.numeric().

Value

Returns an NxK matrix.

Missing values

Both argument X and xTarget may contain non-finite values. These values do not affect the estimation of the normalization function. Non-finite values in X, remain in the output.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

[1] H. Bengtsson, R. Irizarry, B. Carvalho, and T. Speed, *Estimation and assessment of raw copy numbers at the single locus level*, Bioinformatics, 2008.

See Also

 $Internally \verb| normalizeQuantileSpline.numeric()| is used. *normalizeQuantileRank()|.$

```
# Plot the data
layout(matrix(c(1,0,2:5), ncol=2, byrow=TRUE))
xlim <- range(X, na.rm=TRUE);
plotDensity(X, lwd=2, xlim=xlim, main="The three original distributions")

Xn <- normalizeQuantile(X)
plotDensity(Xn, lwd=2, xlim=xlim, main="The three normalized distributions")
plotXYCurve(X, Xn, xlim=xlim, main="The three normalized distributions")

Xn2 <- normalizeQuantileSpline(X, xTarget=Xn[,1], spar=0.99)
plotDensity(Xn2, lwd=2, xlim=xlim, main="The three normalized distributions")
plotXYCurve(X, Xn2, xlim=xlim, main="The three normalized distributions")</pre>
```

normalizeQuantileSpline.numeric

Normalizes the empirical distribution of a single sample to a target distribution

Description

Normalizes the empirical distribution of a single sample to a target distribution.

Usage

```
## S3 method for class 'numeric':
normalizeQuantileSpline(x, w=NULL, xTarget, sortTarget=TRUE, ..., robust=TRUE)
```

Arguments

Value

Returns a numeric vector of length N.

Missing values

Both argument X and xTarget may contain non-finite values. These values do not affect the estimation of the normalization function. Non-finite values in X, remain in the output.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

46 plotDensity.list

References

[1] H. Bengtsson, R. Irizarry, B. Carvalho, and T. Speed, *Estimation and assessment of raw copy numbers at the single locus level*, Bioinformatics, 2008.

See Also

 $\label{line:continuous} Internally\ either\ \verb"robustSmoothSpline" or \verb"smooth.spline" is used. normalizeQuantileSpline.matrix *normalizeQuantileRank().$

```
plotDensity.list Plots density distributions for a set of vector
```

Description

Plots density distributions for a set of vector.

Usage

```
## S3 method for class 'list':
plotDensity(X, xlim=NULL, ylim=NULL, xlab=NULL, ylab="density (integrates to one
```

Arguments

Χ	A single of list of numeric vectors, a numeric matrix, or a numeric data.frame.
xlim,ylim	character vector of length 2. The x and y limits.
xlab,ylab	character string for labels on x and y axis.
col	The color(s) of the curves.
lty	The types of curves.
lwd	The width of curves.
	Additional arguments passed to density, plot, and lines.
add	If TRUE, the curves are plotted in the current plot, otherwise a new is created.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

plotMvsA.matrix 47

```
plotMvsA.matrix Plot log-ratios vs log-intensities
```

Description

Plot log-ratios vs log-intensities.

Usage

```
## S3 method for class 'matrix': plotMvsA(X, Alab="A", Mlab="M", Alim=c(0, 16), Mlim=c(-1, 1) * diff(Alim), pch="
```

Arguments

```
    Nx2 matrix with two channels and N observations.
    Alab, Mlab Labels on the x and y axes.
    Alim, Mlim Plot range on the A and M axes.
    pch Plot symbol used.
    ... Additional arguments accepted by points.
    add If TRUE, data points are plotted in the current plot, otherwise a new plot is created.
```

Details

Red channel is assumed to be in column one and green in column two. Log-ratio are calculated taking channel one over channel two.

Value

Returns nothing.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

```
plotMvsAPairs.matrix
```

Plot log-ratios/log-intensities for all unique pairs of data vectors

Description

Plot log-ratios/log-intensities for all unique pairs of data vectors.

Usage

```
## S3 method for class 'matrix': plotMvsAPairs(X, Alab="A", Mlab="M", Alim=c(0, 16), Mlim=c(-1, 1) * diff(Alim),
```

plotMvsMPairs.matrix

Arguments

Х	$NxK \; \text{matrix} \; \text{where} \; N \; \text{is the number of observations and} \; K \; \text{is the number of channels.}$
Alab,Mlab	Labels on the x and y axes.
Alim, Mlim	Plot range on the A and M axes.
pch	Plot symbol used.
	Additional arguments accepted by points.
add	If TRUE, data points are plotted in the current plot, otherwise a new plot is created.

Details

Log-ratios and log-intensities are calculated for each neighboring pair of channels (columns) and plotted. Thus, in total there will be K-1 data set plotted.

The colors used for the plotted pairs are 1, 2, and so on. To change the colors, use a different color palette.

Value

Returns nothing.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

```
plotMvsMPairs.matrix
```

Plot log-ratios vs log-ratios for all pairs of columns

Description

Plot log-ratios vs log-ratios for all pairs of columns.

Usage

```
## S3 method for class 'matrix':
plotMvsMPairs(X, xlab="M", ylab="M", xlim=c(-1, 1) * 6, ylim=xlim, pch=".", ...,
```

Arguments

X	Nx2Kmatrix where N is the number of observations and $2K$ is an even number of channels.
xlab,ylab	Labels on the x and y axes.
xlim,ylim	Plot range on the x and y axes.
pch	Plot symbol used.
	Additional arguments accepted by points.
add	If TRUE, data points are plotted in the current plot, otherwise a new plot is created.

plotXYCurve.matrix 49

Details

Log-ratio are calculated by over paired columns, e.g. column 1 and 2, column 3 and 4, and so on.

Value

Returns nothing.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

plotXYCurve.matrix Plot the relationship between two variables as a smooth curve

Description

Plot the relationship between two variables as a smooth curve.

Usage

```
## S3 method for class 'matrix':
plotXYCurve(X, Y, col=1:nrow(X), lwd=NULL, xlim=NULL, ylim=xlim, xlab=NULL, ylab
```

Arguments

Value

Returns (invisibly) the curve fit.

Missing values

Data points (x,y) with non-finite values are excluded.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

See Also

Internally plotXYCurve.numeric() is used.

plotXYCurve.numeric

```
plotXYCurve.numeric
```

Plot the relationship between two variables as a smooth curve

Description

Plot the relationship between two variables as a smooth curve.

Usage

```
## S3 method for class 'numeric':
plotXYCurve(x, y, lwd=2, col=1, dlwd=1, dcol=NA, xlim=NULL, ylim=xlim, xlab=NULI
```

Arguments

х, у	Two numeric vector of length N.
lwd	The width of the curve.
col	The color of the curve.
dlwd	The width of the density curves.
dcol	The fill color of the interior of the density curves.
xlim, ylim	The x and y plotting limits.
xlab, ylab	The x and y labels.
curveFit	The function used to fit the curve. The two first arguments of the function must take x and y , and the function must return a list with fitted elements x and y .
	Additional arguments passed to lines used to draw the curve.
add	If TRUE, the graph is added to the current plot, otherwise a new plot is created.

Value

Returns (invisibly) the curve fit.

Missing values

Data points (x,y) with non-finite values are excluded.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

See Also

```
plotXYCurve.matrix().
```

```
print.SmoothSplineLikelihood

Prints an SmoothSplineLikelihood object
```

Description

Prints an SmoothSplineLikelihood object. A SmoothSplineLikelihood object is returned by likelihood.smooth.splineLikelihood.splineLike

Usage

```
## S3 method for class 'SmoothSplineLikelihood':
print(x, digits=getOption("digits"), ...)
```

Arguments

```
x Object to be printed.digits Minimal number of significant digits to print.... Not used.
```

Value

Returns nothing.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

robustSmoothSpline Robust fit of a Smoothing Spline

Description

Fits a smoothing spline robustly using the L_1 norm. Currently, the algorithm is an *iterative reweighted* smooth spline algorithm which calls smooth.spline (x, y, w, . . .) at each iteration with the weights we equal to the inverse of the absolute value of the residuals for the last iteration step.

Usage

```
## Default S3 method:
robustSmoothSpline(x, y=NULL, w=NULL, ..., minIter=3, maxIter=max(minIter, 50),
```

52 robustSmoothSpline

Arguments

х	a vector giving the values of the predictor variable, or a list or a two-column matrix specifying x and y. If x is of class smooth.spline then $x \le x$ is used as the x values and $x \le y$ in are used as the y values.
У	responses. If y is missing, the responses are assumed to be specified by x .
W	a vector of weights the same length as x giving the weights to use for each element of x . Default value is equal weight to all values.
	Other arguments passed to smooth.spline.
minIter	the minimum number of iterations used to fit the smoothing spline robustly. Default value is 3.
maxIter	the maximum number of iterations used to fit the smoothing spline robustly. Default value is 25.
sdCriteria	Convergence criteria, which the difference between the standard deviation of the residuals between two consecutive iteration steps. Default value is 2e-4.
reps	Small positive number added to residuals to avoid division by zero when calculating new weights for next iteration.
plotCurves	If TRUE, the fitted splines are added to the current plot, otherwise not.

Value

Returns an object of class smooth.spline.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

See Also

```
smooth.spline.
```

```
data(cars)
attach(cars)
plot(speed, dist, main = "data(cars) & robust smoothing splines")

# Fit a smoothing spline using L_2 norm
cars.spl <- smooth.spline(speed, dist)
lines(cars.spl, col = "blue")

# Fit a smoothing spline using L_1 norm
cars.rspl <- robustSmoothSpline(speed, dist)
lines(cars.rspl, col = "red")

# Fit a smoothing spline using L_2 norm with 10 degrees of freedom
lines(smooth.spline(speed, dist, df=10), lty=2, col = "blue")

# Fit a smoothing spline using L_1 norm with 10 degrees of freedom
lines(robustSmoothSpline(speed, dist, df=10), lty=2, col = "red")

legend(5,120, c(
    paste("smooth.spline [C.V.] => df = ",round(cars.spl$df,1)),
```

```
paste("robustSmoothSpline [C.V.] => df =",round(cars.rspl$df,1)),    "standard with s( * , df = 10)", "robust with s( * , df = 10)"), col = c("blue","red","blue","red"), lty = c(1,1,2,2), bg='bisque')
```

sampleCorrelations.matrix

Calculates the correlation for random pairs of observations

Description

Calculates the correlation for random pairs of observations.

Usage

```
## S3 method for class 'matrix':
sampleCorrelations(X, MARGIN=1, pairs=NULL, npairs=max(5000, nrow(X)), ...)
```

Arguments

X	An NxK matrix where $N \ge 2$ and $K \ge 2$.
MARGIN	The dimension (1 or 2) in which the observations are. If $MARGIN==1$ (==2), each row (column) is an observation.
pairs	If a Lx2 matrix, the L index pairs for which the correlations are calculated. If NULL, pairs of observations are sampled.
npairs	The number of correlations to calculate.
	Not used.

Value

Returns a double vector of length npairs.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

[1] A. Ploner, L. Miller, P. Hall, J. Bergh & Y. Pawitan. *Correlation test to assess low-level processing of high-density oligonucleotide microarray data*. BMC Bioinformatics, 2005, vol 6.

See Also

```
sample().
```

```
# Simulate 20000 genes with 10 observations each
X <- matrix(rnorm(n=20000), ncol=10)

# Calculate the correlation for 5000 random gene pairs
cor <- sampleCorrelations(X, npairs=5000)
print(summary(cor))</pre>
```

54 sampleTuples

sampleTuples

Sample tuples of elements from a set

Description

Sample tuples of elements from a set. The elements within a sampled tuple are unique, i.e. no two elements are the same.

Usage

```
## Default S3 method:
sampleTuples(x, size, length, ...)
```

Arguments

x A set of elements to sample from.
size The number of tuples to sample.
length The length of each tuple.
... Additional arguments passed to sample().

Value

Returns a NxK matrix where N =size and K =length.

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

See Also

```
sample().
```

```
pairs <- sampleTuples(1:10, size=5, length=2)
print(pairs)

triples <- sampleTuples(1:10, size=5, length=3)
print(triples)

# Allow tuples with repeated elements
quadruples <- sampleTuples(1:3, size=5, length=4, replace=TRUE)
print(quadruples)</pre>
```

weightedMedian 55

htedMedian Weighted Median Value	weightedMedian Weighted Median Value
----------------------------------	--------------------------------------

Description

Computes a weighted median of a numeric vector.

Usage

```
## Default S3 method:
weightedMedian(x, w, na.rm=NA, interpolate=is.null(ties), ties=NULL, method=c("c
```

Arguments

guments	
Х	a numeric vector containing the values whose weighted median is to be computed.
W	a vector of weights the same length as x giving the weights to use for each element of x . Negative weights are treated as zero weights. Default value is equal weight to all values.
na.rm	a logical value indicating whether NA values in \times should be stripped before the computation proceeds, or not. If NA, no check at all for NAs is done. Default value is NA (for effiency).
interpolate	If TRUE, linear interpolation is used to get a consistant estimate of the weighted median.
ties	If interpolate == FALSE, a character string specifying how to solve ties between two x's that are satisfying the weighted median criteria. Note that at most two values can satisfy the criteria. When ties is "min", the smaller value of the two is returned and when it is "max", the larger value is returned. If ties is "mean", the mean of the two values is returned and if it is "both", both values are returned. Finally, if ties is "weighted" (or NULL) a weighted average of the two are returned, where the weights are weights of all values $x[i] \le x[k]$ and $x[i] \ge x[k]$, respectively.
method	If "shell", then order() is used and when $method="quick"$, then internal qsort() is used.
	Not used.

Details

For the n elements $x = c(x[1], x[2], \ldots, x[n])$ with positive weights $w = c(w[1], w[2], \ldots, w[n])$ such that sum(w) = S, the *weighted median* is defined as the element x[k] for which the total weight of all elements x[i] < x[k] is less or equal to S/2 and for which the total weight of all elements x[i] > x[k] is less or equal to S/2 (c.f. [1]).

If w is missing then all elements of x are given the same positive weight. If all weights are zero, NA is returned.

If one or more weights are Inf, it is the same as these weights have the same weight and the others has zero. This makes things easier for cases where the weights are result of a division with zero. In this case median() is used internally.

When all the weights are the same (after values with weight zero are excluded and Inf's are taken care of), median is used internally.

56 weightedMedian

The weighted median solves the following optimization problem:

$$\alpha^* = \arg_{\alpha} \min \sum_{k=1} Kw_k |x_k - \alpha|$$

where $x = (x_1, x_2, \dots, x_K)$ are scalars and $w = (w_1, w_2, \dots, w_K)$ are the corresponding "weights" for each individual x value.

Value

Returns the weighted median.

Benchmarks

When implementing this function speed has been highly prioritized and it also making use of the internal quick sort algorithm (from R v1.5.0). The result is that weightedMedian(x) is about half as slow as median(x). It is hard to say how much since it depends on the data set, but it is also hard to time it exactly since internal garbage collector etc might mess up the measurements.

Initial test also indicates that method="shell", which uses order() is slower than method="quick", which uses internal qsort(). Non-weighted median can use partial sorting which is faster because all values do not have to be sorted.

See examples below for some simple benchmarking tests.

Author(s)

Henrik Bengtsson and Ola Hössjer, Centre for Mathematical Sciences, Lund University. Thanks to Roger Koenker, Econometrics, University of Illinois, for the initial ideas.

References

[1] T.H. Cormen, C.E. Leiserson, R.L. Rivest, Introduction to Algorithms, The MIT Press, Massachusetts Institute of Technology, 1989.

See Also

median, mean() and weighted.mean.

```
x <- 1:10
n \leftarrow length(x)
m1 <- median(x)
                                                # 5.5
m2 <- weightedMedian(x)</pre>
                                                # 5.5
stopifnot(identical(m1, m2))
w \leftarrow rep(1, n)
m1 <- weightedMedian(x, w)</pre>
                                               # 5.5 (default)
m2 \leftarrow weightedMedian(x, ties="weighted") # 5.5 (default)
m3 <- weightedMedian(x, ties="min")</pre>
                                               # 5
m4 <- weightedMedian(x, ties="max")</pre>
                                               # 6
stopifnot(identical(m1, m2))
# Pull the median towards zero
w[1] < -5
```

```
m1 <- weightedMedian(x, w)</pre>
                                             # 3.5
y <- c(rep(0, w[1]), x[-1])
                                             # Only possible for integer weights
m2 <- median(y)</pre>
                                             # 3.5
stopifnot(identical(m1, m2))
# Put even more weight on the zero
w[1] < -8.5
weightedMedian(x, w)
                                       # 2
# All weight on the first value
w[1] \leftarrow Inf
weightedMedian(x, w)
                                       # 1
# All weight on the last value
w[1] < -1
w[n] \leftarrow Inf
                                       # 10
weightedMedian(x, w)
# All weights set to zero
w \leftarrow rep(0, n)
weightedMedian(x, w)
                                       # NA
# Simple benchmarking
bench <- function(N=1e5, K=10) {
  x <- rnorm(N)
  t <- c()
  gc()
  t[1] \leftarrow system.time(for (k in 1:K) median(x))[3]
  t[2] <- system.time(for (k in 1:K) weightedMedian(x, method="quick"))[3]
  ac()
  t[3] <- system.time(for (k in 1:K) weightedMedian(x, method="shell"))[3]
  t < -t / t[1]
  t[4] \leftarrow t[2]/t[3]
  names(t) <- c("median", "wMed-quick", "wMed-shell", "quick/shell")</pre>
}
print(bench(N= 5, K=1000))
print(bench(N=100, K=1000))
print(bench(N=1e3, K=100))
print(bench(N=1e5, K=10))
print(bench(N=1e6, K=1))
```

wpca.matrix

Light-weight Weighted Principal Component Analysis

Description

Calculates the (weighted) principal components of a matrix, that is, finds a new coordinate system (not unique) for representing the given multivariate data such that i) all dimensions are orthogonal to each other, and ii) all dimensions have maximal variances.

Usage

```
## S3 method for class 'matrix':
wpca(x, w=NULL, center=TRUE, scale=FALSE, method=c("dgesdd", "dgesvd", "dsvdc"),
```

Arguments

x An NxK matrix.

w An N vector of weights for each row (observation) in the data matrix. If

NULL, all observations get the same weight, that is, standard PCA is used.

center If TRUE, the (weighted) sample mean column vector is subtracted from each

column in mat, first. If data is not centered, the effect will be that a linear

subspace that goes through the origin is fitted.

scale If TRUE, each column in mat is divided by its (weighted) root-mean-square of

the centered column, first.

method If "dgesdd" LAPACK's divide-and-conquer based SVD routine is used (faster

[1]), if "dgesvd", LAPACK's QR-decomposition-based routine is used, and if "dsvdc", LINPACK's DSVDC(?) routine is used. The latter is just for pure

backward compatibility with R v1.7.0.

swapDirections

If TRUE, the signs of eigenvectors that have more negative than positive components are inverted. The signs of corresponding principal components are also inverted. This is only of interest when for instance visualizing or comparing with other PCA estimates from other methods, because the PCA (SVD) decom-

postion of a matrix is not unique.

... Not used.

Value

Returns a list with elements:

pc An NxK matrix where the column vectors are the principal components

(a.k.a. loading vectors, spectral loadings or factors etc).

d An K vector containing the eigenvalues of the principal components.

vt An KxK matrix containing the eigenvector of the principal components.

xMean The center coordinate.

It holds that x == t(t(fit\$pc %*% fit\$vt) + fit\$xMean).

Method

A singular value decomposition (SVD) is carried out. Let X=mat, then the SVD of the matrix is X=UDV', where U and V are othogonal, and D is a diagonal matrix with singular values. The principal returned by this method are UD.

Internally La.svd() (or svd()) of the **base** package is used. For a popular and well written introduction to SVD see for instance [2].

Author(s)

```
Henrik Bengtsson (http://www.braju.com/R/)
```

References

```
[1] J. Demmel and J. Dongarra, DOE2000 Progress Report, 2004. http://www.cs.berkeley.edu/~demmel/DOE2000/Report0100.html
[2] Todd Will, Introduction to the Singular Value Decomposition, UW-La Crosse, 2004. http://www.uwlax.edu/faculty/will/svd/
```

See Also

For a iterative re-weighted PCA method, see *iwpca(). For Singular Value Decomposition, see svd(). For other implementations of Principal Component Analysis functions see (if they are installed): prcomp (stats) and pca (pcurve).

```
for (zzz in 0) {
# This example requires plot3d() in R.basic [http://www.braju.com/R/]
if (!require(R.basic)) break
# A first example
# -----
\# Simulate data from the model y <- a + bx + eps(bx)
x < - rexp(1000)
a < -c(2, 15, 3)
b < -c(2,3,15)
bx <- outer(b,x)
eps <- apply(bx, MARGIN=2, FUN=function(x) rnorm(length(x), mean=0, sd=0.1*x))
y \leftarrow a + bx + eps
y <- t(y)
# Add some outliers by permuting the dimensions for 1/3 of the observations
idx <- sample(1:nrow(y), size=1/3*nrow(y))</pre>
y[idx,] \leftarrow y[idx,c(2,3,1)]
\# Down-weight the outliers W times to demonstrate how weights are used
W <- 10
# Plot the data with fitted lines at four different view points
N <- 4
theta \leftarrow seq(0,180,length=N)
phi <- rep(30, length.out=N)</pre>
# Use a different color for each set of weights
col <- topo.colors(W)</pre>
opar <- par(mar=c(1,1,1,1)+0.1)
layout(matrix(1:N, nrow=2, byrow=TRUE))
for (kk in seq(theta)) {
  # Plot the data
 plot3d(y, theta=theta[kk], phi=phi[kk])
  # First, same weights for all observations
  w <- rep(1, length=nrow(y))</pre>
```

```
for (ww in 1:W) {
    # Fit a line using IWPCA through data
   fit <- wpca(y, w=w, swapDirections=TRUE)</pre>
   # Get the first principal component
   ymid <- fit$xMean</pre>
   d0 <- apply(y, MARGIN=2, FUN=min) - ymid
   d1 <- apply(y, MARGIN=2, FUN=max) - ymid
   b <- fit$vt[1,]
   y0 < -b * max(abs(d0))
   y1 \leftarrow b * max(abs(d1))
   yline <- matrix(c(y0,y1), nrow=length(b), ncol=2)
   yline <- yline + ymid
   points3d(t(ymid), col=col)
   lines3d(t(yline), col=col)
   # Down-weight outliers only, because here we know which they are.
   w[idx] \leftarrow w[idx]/2
  # Highlight the last one
  lines3d(t(yline), col="red", lwd=3)
par(opar)
} # for (zzz in 0)
rm(zzz)
 if (dev.cur() > 1) dev.off()
  # -----
# A second example
# -----
# Data
x < -c(1,2,3,4,5)
y < -c(2,4,3,3,6)
opar <- par(bty="L")</pre>
opalette <- palette(c("blue", "red", "black"))</pre>
xlim \leftarrow ylim \leftarrow c(0,6)
# Plot the data and the center mass
plot(x,y, pch=16, cex=1.5, xlim=xlim, ylim=ylim)
points(mean(x), mean(y), cex=2, lwd=2, col="blue")
# Linear regression y ~ x
fit <-lm(y \sim x)
abline(fit, lty=1, col=1)
# Linear regression y ~ x through without intercept
fit <-lm(y \sim x - 1)
abline(fit, lty=2, col=1)
# Linear regression x ~ y
fit <-lm(x \sim y)
```

```
c <- coefficients(fit)</pre>
b < -1/c[2]
a <- -b*c[1]
abline(a=a, b=b, lty=1, col=2)
\# Linear regression x \sim y through without intercept
fit <-lm(x \sim y - 1)
b <- 1/coefficients(fit)</pre>
abline(a=0, b=b, lty=2, col=2)
# Orthogonal linear "regression"
fit <- wpca(cbind(x,y))</pre>
b <- fit$vt[1,2]/fit$vt[1,1]</pre>
a <- fit$xMean[2]-b*fit$xMean[1]</pre>
abline(a=a, b=b, lwd=2, col=3)
# Orthogonal linear "regression" without intercept
fit <- wpca(cbind(x,y), center=FALSE)
b <- fit$vt[1,2]/fit$vt[1,1]</pre>
a <- fit$xMean[2]-b*fit$xMean[1]</pre>
abline(a=a, b=b, lty=2, lwd=2, col=3)
legend(xlim[1],ylim[2], legend=c("lm(y~x)", "lm(y~x-1)", "lm(x~y)",
           "lm(x\sim y-1)", "pca", "pca w/o intercept"), lty=rep(1:2,3),
                       lwd=rep(c(1,1,2),each=2), col=rep(1:3,each=2))
palette(opalette)
par(opar)
```

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