# GlobalAncova with Special Sum of Squares Decompositions

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### 1 Abstract

This vignette shows the enhancements made for *GlobalAncova*. Basically, there are four ideas implemented:

- decomposition of the sum of squares of a linear model ([2])
- a plotting function for the sequential decomposition
- pairwise comparison for factor levels
- adjustment for global covariates

The decomposition of the model sum of squares results in an ANOVA table, which shows the sum of squares due to each term of a linear model. It can be used either on a global basis or for a small group of genes on a gene-wise basis. Pairwise comparisons allow conclusions about whether or not the gene expressions of two levels of a factor are significantly different. An adjustment for global covariates is possible in cases where not only one but two expression sets per subject exist. If the second set describes the subject's 'normal' status, it can be used to reduce the variance between subjects.

Since a permutation approach is not (yet) implemented as it is in the basic GlobalAncova function, the functionalities described in this vignette may be seen like rather descriptive tools. Large p-values indicate that there is no significant effect, whereas small p-values have to interpreted with caution. Appropriate p-values for testing any linear hypothesis about phenotype effects can be derived using the basic function GlobalAncova.

This document was created using R version 2.7.0 and version 3.6.0 of the GlobalAncova package.

### 2 Sequential and Type III Decomposition

Decomposition of sum of squares (SSQ) can be used so as to show the effect of each factor of a linear model on the gene expression. Two types of decomposition of the model SSQ are presented here: the sequential and the type III decomposition. Both are computed using the extra sum of squares principle repeatedly, yet they have different approaches with regard to which factors are to be kept or to be left out. For both decompositions an F-test can be performed. The two methods are implemented in the function GlobalAncova.decomp and can be selected by specifying the argument method, which can be either one of "sequential" (default), "type3" or "all". The latest yields a list of both. Other arguments to GlobalAncova.decomp are xx specifying the expression matrix, formula describing the model to be decomposed and model.dat determining phenotype data. The names or indices of the group of genes to be analysed can be set in the test.genes parameter.

#### Sequential Decomposition

In the sequential or hierarchical decomposition, the sum of squares of each term of the model are calculated by adding to the model term after term and obtaining the increase in model SSQ due the addition. Thus, each term is adjusted for all preceding terms but not for the succeeding ones. Consequently, the order of terms in the model is important as the following examples show. Applying an Ftest to the sequential SSQ is only meaningful if a logical or hierarchical order of factors exists (e.g. main effects first followed by interaction effects). Only in this case, it can be tested when the factors start to be insignificant. The following examples are based on the van't Veer breast cancer data set [3], which is included in the Global Ancova package. A subset of the data consisting of the expression values for 96 patients without BRCA1 or BRCA2 mutations is available. The dataset (vantVeer) is restricted to 1113 genes associated with 9 cancer related pathways that are provided as a list named pathways. The phenotype data of this study (phenodata) include the grade of the tumour (grade), whether or not metastases were developed (metastases) and the estrogen receptor status (ERstatus). Giving the assumption that all three factors measured have an effect on gene expression, a possible linear model for the gene expressions could be

- > library(GlobalAncova)
- > data(vantVeer)
- > data(phenodata)
- > data(pathways)

### > formula <- ~grade + metastases + ERstatus

We will now investigate which of the terms of the former model have effects on the overall gene expression.

```
> GlobalAncova.decomp(xx = vantVeer, formula = formula,
+ model.dat = phenodata, method = "sequential")
```

	SSQ	df	MS	F	p
Intercept	443.62541	1113	0.39858527	9.776182	0.000000e+00
grade	194.50524	2226	0.08737881	2.143158	4.095934e-180
metastases	53.97303	1113	0.04849329	1.189405	1.325949e-05
ERstatus	209.86860	1113	0.18856118	4.624878	0.000000e+00
error	4129.41514	101283	0.04077106	NA	NA

Apparently, all factors of the model are significant. Note however, that since expressions are correlated and have non-normal distribution, the p-values derived from the F-distribution lead to alpha-inflation.

In oder to demonstrate the impact of the order of terms we will repeat the analysis using the same model but in reverse order.

```
> formula2 <- ~ERstatus + metastases + grade
> GlobalAncova.decomp(xx = vantVeer, formula = formula2,
+ model.dat = phenodata, method = "sequential")
```

	SSQ	df	MS	F	p
Intercept	443.62541	1113	0.39858527	9.776182	0.000000e+00
ERstatus	269.99053	1113	0.24257909	5.949786	0.000000e+00
metastases	63.67287	1113	0.05720833	1.403160	1.822444e-17
grade	124.68347	2226	0.05601234	1.373826	1.131387e-28
error	4129.41514	101283	0.04077106	NA	NA

Differences in sum of squares due to different ordering of terms indicate a non-orthogonal design matrix. One major property of the sequential method is that the sums of squares due to the single terms add up to the full model SSQ. This is not generally the case in the type III decomposition.

### Type III Decomposition

In contrast to the sequential decomposition, the type III decomposition is calculated by removing only a single term at a time from the full model. That is, every term is adjusted for every other term in the model and is thus treated as if ordered last. To select the type III sum of squares the option method = "type3" has to be set. The terms of the model derived from the van't Veer dataset can now be tested by using the following call

```
> GlobalAncova.decomp(xx = vantVeer, formula = formula,
+ model.dat = phenodata, method = "type3")
```

	SSQ	df	MS	F	p
Intercept	186.06742	1113	0.16717648	4.100371	0.000000e+00
grade	124.68347	2226	0.05601234	1.373826	1.131387e-28
${\tt metastases}$	47.70751	1113	0.04286389	1.051331	1.154727e-01
ERstatus	209.86860	1113	0.18856118	4.624878	0.000000e+00
error	4129.41514	101283	0.04077106	NΑ	NA

The SSQ due to the last term is the same in both decompositions. All terms but the last have generally smaller type III than sequential sums of squares. Only in case of an orthogonal design matrix they have equal sums of squares in both decompositions. This examples demonstrates how important the adjustment for more than one phenotype—characterizing covariate can be. Besides the occurrence of metastases, grade and estrogen receptor status contribute substantially to the observed differential gene expressions.

### 3 Testing Groups of Genes

In some studies, the interest lies not with the entire expression matrix but only with certain groups of genes, e.g. pathways. The names or indices of these genes can be specified in the option *test.genes*. As example, we use the first three cancer relevant pathways given in the object pathways.

```
> GlobalAncova.decomp(xx = vantVeer, formula = formula,
      model.dat = phenodata, method = "type3", test.genes = pathways[1:3])
$androgen_receptor_signaling
                  SSQ
                         дf
                                    MS
                                                 F
                                                                р
Intercept
            31.070643
                         72 0.43153671 12.4661789 2.060236e-132
grade
             9.448638
                        144 0.06561554
                                        1.8954937
             1.568993
                         72 0.02179157 0.6295123
                                                    9.939806e-01
metastases
                         72 0.40451549 11.6855933 1.671092e-122
ERstatus
            29.125115
error
           226.807952 6552 0.03461660
                                                NA
                                                               NA
$apoptosis
                                                F
                   SSQ
                          df
                                     MS
Intercept
            33.073033
                         187 0.17686114 5.350719 3.067227e-107
grade
            16.433991
                         374 0.04394115 1.329386
                                                   2.488033e-05
             6.267846
                         187 0.03351789 1.014043
                                                   4.331773e-01
metastases
                         187 0.24420811 7.388220 1.799784e-172
ERstatus
            45.666917
error
           562.475084 17017 0.03305372
                                               NA
                                                              NA
$cell_cycle_control
                                               F
                                    MS
                                                             p
                         31 0.13464512 3.268404 3.399027e-09
Intercept
              4.173999
grade
             8.024304
                         62 0.12942426 3.141672 5.765491e-15
metastases
             1.397575
                         31 0.04508307 1.094356 3.295908e-01
ERstatus
            10.863558
                         31 0.35043735 8.506590 9.911064e-37
           116.213873 2821 0.04119598
                                                            NA
error
                                              NΑ
```

Estrogen receptor status and tumour grade are significant in all three pathways, whereas the indicator of the development of metastases is not significant in any of them.

### Gene-wise Analysis

For a more detailed analysis, it is furthermore possible to display the sequential decomposition for each gene seperately. Due to the large numerical output, this option will only be interesting for a limited number of genes. It can be chosen by setting genewise=TRUE. This option also serves the purpose of providing a nummerical view of what is shown by the function Plot.sequential, see section 4. Just for demonstration we will show the gene-wise result of the sequential decomposition for the first three genes of the first pathway.

```
> GlobalAncova.decomp(xx = vantVeer, formula = formula,
      model.dat = phenodata, test.genes = pathways[[1]][1:3],
      genewise = TRUE)
$terms
[1] "Intercept"
                               "metastases" "ERstatus"
                 "grade"
                                                         "error"
$SSQ
          Intercept
                                 metastases
                                               ERstatus
                         grade
                                                           error
AW025529
         0.0047040 0.12624647 0.0639334130 0.19956603 2.116086
NM_001648 0.1137127 0.04911051 0.0016380351 0.03591376 2.068737
NM_001753 0.1944000 0.47020168 0.0001075029 0.07604684 4.033718
all
          0.3128167 0.64555866 0.0656789509 0.31152663 8.218541
$df
     Intercept grade metastases ERstatus error
gene
                   2
                                        1
                                             91
             1
                              1
             3
                   6
all
                              3
                                        3
                                            273
$MS
          Intercept
                         grade
                                 metastases
                                               ERstatus
                                                             error
AW025529
          0.0047040 0.06312324 0.0639334130 0.19956603 0.02325369
NM_001648 0.1137127 0.02455526 0.0016380351 0.03591376 0.02273337
NM_001753 0.1944000 0.23510084 0.0001075029 0.07604684 0.04432657
          0.1042722 0.10759311 0.0218929836 0.10384221 0.03010455
all
$F
          Intercept
                       grade metastases ERstatus
AW025529 0.2022904 2.714547 2.749387475 8.582122
NM_001648 5.0020145 1.080141 0.072054202 1.579781
NM_001753 4.3856313 5.303835 0.002425247 1.715604
          3.4636703 3.573982 0.727231813 3.449386
all
$р
                           grade metastases
           Intercept
                                                ERstatus
AW025529 0.65394791 0.071600418 0.1007351 0.004290456
NM_001648 0.02776149 0.343860324
                                  0.7889766 0.212008777
NM_001753 0.03902333 0.006625639
                                  0.9608305 0.193556935
          0.01681092 0.001998268
                                  0.5364938 0.017132770
```

# 4 Diagnostic Plots

In this section a graphical method will be introduced to visualize the result of genewise sequential decomposition. This graphic can either be plotted on its own or in combination with the function Plot.genes, see *GlobalAncova* vignette.

The function Plot.sequential yields a bar plot with bars for the single genes and one for the over all result. The segments of the bars indicate the extra sum of squares due to each factor relative to the model SSQ of the corresponding gene. In order to enable an easier comparison between the genes, the model SSQ of each gene is set to 1. The arguments to this function are the expression matrix xx, the formula of the model to be decomposed, the phenotype data model.dat and optionally a vector of gene names or indices test.genes specifying the gene set and the name of the gene set name.geneset (for the title of the plot). As an example we will investigate the structure of the cell cycle pathway genes from the van't Veer study, see figure 1.

```
> Plot.sequential(vantVeer, formula = ~ERstatus + metastases +
+ grade, model.dat = phenodata, test.genes = pathways[[3]],
+ name.geneset = "cell cycle pathway")
```

#### Sequential Sum of Squares cell cycle pathway

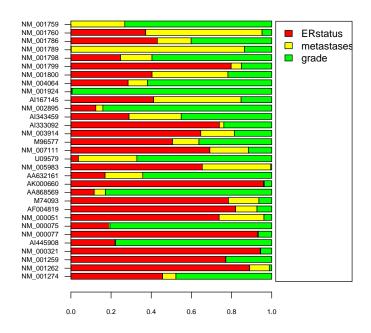


Figure 1: Sequential decomposition of model sum of squares for the cell cycle genes in the van't Veer data.

In order to gain information about the significance of the factors, it is also possible to combine the former plot with the *GlobalAncova* gene plot. The gene plot shows for two given models the gene-wise extra sum of squares and the mean square error in a barplot. In the combined plot, the gene plot is used to show the extra sum of squares due to all factors of the model altogether. Hence, not only the decomposition can be visualized but also the significance of the full

model for each gene. For displaying again the effects on the cell cycle genes in the van't Veer data with the combined plot (figure 2) we use

```
> Plot.all(vantVeer, formula = ~ERstatus + metastases +
+ grade, model.dat = phenodata, test.genes = pathways[[3]],
+ name.geneset = "cell cycle pathway")
```

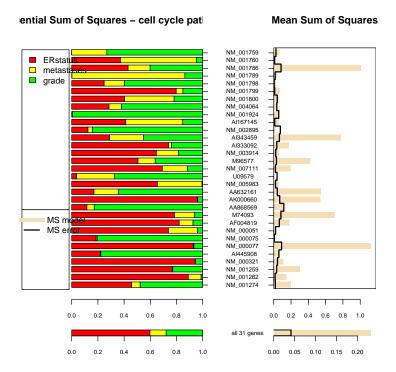


Figure 2: Sequential decomposition of model sum of squares and model mean squares for the cell cycle genes in the van't Veer data.

From figure 2 we can conclude, that effects of the model terms vary from gene to gene. ERstatus seems to play a major role, however one has to remember, that a sequential decomposition is displayed and ERstatus was ordered first. This question could be answered by using a different order for the model formula. Most importantly, the graph on the left can be used for understanding the significane of the model displayed on the right hand graph. This graphical method helps to investigate a lot of different and complex models, e.g. differential co-expression.

## 5 Pairwise Comparisons of Factor Levels

Some studies focus on the connection between a single factor and gene expression. This is, for instance, the case when the factor in question provides some kind of classification. To investigate how a classification is reflected in the gene

expression, pair-wise comparisons of factor levels can be used. The method presented here analyses for a pair of factor levels whether the genes under observation are diffentely expressed, i.e. it can detect whether the difference between two levels is reflected in the gene expression. As measurement for the extra sum of squares due to this difference, the method uses the decrease in residual sum of squares obtained when the two are set to the same level. Pairwise comparisons can be performed by using the function pair.compare. Similarly to the function GlobalAncova.decomp, pair.compare requires the arguments xx (expression matrix), formula (model) and model.dat (phenotype data). Furthermore, the argument group has to be set to the name of the factor which is to be analysed. The function yields an ANOVA table with a row for each possible combination of the factor levels. Since pair-wise comparison is a multiple testing problem, not only the p-values based on the permutation test are returned but also the Bonferroni-Holm adjusted p-values.

As an example we will perform pair-wise comparisons of the three levels of tumour grade in the van't Veer data.

```
> pair.compare(xx = vantVeer, formula = ~grade, model.dat = phenodata,
+ group = "grade", perm = 100)
```

```
SSQ
                     df
                                 MS
                                            F p.perm
1:2
        43.80796
                   1113 0.03936025 0.9273622
                                                0.64
1:3
       103.10757
                   1113 0.09263932 2.1826641
                                                0.00
2:3
       114.99741
                   1113 0.10332202 2.4343578
                                                0.00
error 4393.25676 103509 0.04244323
                                           NA
                                                  NA
```

There are essential differences between stages 1 and 3 and 2 and 3, respectively, whereas stages 1 and 2 seem to be rather similar.

# 6 Adjusting for a Global Covariate

Considerable variability between patients is the rule in medical statistics. Therefore, adjustment for covariates is often applied so as to reduce variance. Natural candidates for adjustement are covariates representing the baseline status of patients. For microarray data, gene expressions from normal (non-cancer) tissue of a patient might play this role of giving baseline status, which can then be compared to the tumour probe of the same patient. Analogously, tumour probes of a former biopsy might be used to trace changes.

The adjustment for covariates is also implemented in the GlobalAncova.decomp call. It uses the arguments zz and zz.per.gene. The former defines the expression matrix of the global covariate, and the later is a logical value specifying whether or not different parameters should be used for each gene.

The data for the following examples are taken from the colon cancer study of [1]. In this study, tumour as well as normal tissue expressions were measured. Just for demonstration we picked a set of 1747 genes which are associated with cell proliferation and which are measured in tumour and normal tissue of 12 colon cancer patients. The most important factors considered are the carcinoma stage (UICC.stage), the gender (sex) and the location of the tumour (distal/proximal). At first a type III decomposition will be performed only for the tumour data in order to show potential differences made by the later adjustment:

```
> data(colon.tumour)
```

- > data(colon.normal)
- > data(colon.pheno)
- > formula <- ~UICC.stage + sex + location
- > GlobalAncova.decomp(xx = colon.tumour, formula = formula,
- + model.dat = colon.pheno, method = "type3")

```
SSQ
                                       MS
                                                      F
                           df
                        1747 425.0303241 2345.1917477 0.00000000
Intercept 742527.9761
              242.3041
UICC.stage
                         1747
                                0.1386973
                                             0.7652905 1.00000000
sex
              269.6725
                        1747
                                0.1543632
                                             0.8517306 0.99999380
              339.0278 1747
                                              1.0707814 0.02669185
location
                                0.1940628
error
             2532.9374 13976
                                0.1812348
                                                     NA
                                                                NΑ
```

In this analysis neither UICC stage nor sex seem to have an influence on gene expression. We will see wehter this conclusion remains true after adjustment. In order to adjust for the expression in normal state the of cells, intuitively we could use the difference between tumour and normal tissue expression for analysis:

```
> GlobalAncova.decomp(xx = colon.tumour - colon.normal,
+ formula = formula, model.dat = colon.pheno, method = "type3")
```

```
SSQ
                        df
                                  MS
                                             F
Intercept 2062.5365
                     1747 1.1806162 4.5956873 0.00000000
UICC.stage 459.3349
                      1747 0.2629278 1.0234775 0.25531679
            428.9081
                     1747 0.2455112 0.9556814 0.89368340
            482.5561
                     1747 0.2762199 1.0752183 0.02022423
location
           3590.3861 13976 0.2568965
error
                                            NΑ
```

In this example the adjustment does not yield a significant difference to the previous result. Note however, that for the UICC status a considerable reduction in p-value is achieved (see *type3* results).

### Adjustment by using one parameter for all genes

A more general way is to adjust by  $xx - \beta \cdot zz$  allowing  $\beta$  to be different from 1. The parameter  $\beta$  is estimated as the least square estimate of the model  $xx = \beta \cdot zz$ . Thus, we account for a relatively different ground level in the two expression sets. This kind of adjustment can be chosen by specifying zz as the gene expression matrix of the global covariate:

```
> GlobalAncova.decomp(xx = colon.tumour, formula = formula,
+ model.dat = colon.pheno, method = "all", zz = colon.normal)
```

### \$adjustment

ssq df adjustment 2017200 1

### \$sequential

SSQ df MS F p
Intercept 4779.2569 1747 2.7356937 10.6058621 0.00000000

```
UICC.stage 374.1633 1747 0.2141747 0.8303224 0.99999978
sex
            431.1914
                      1747 0.2468182 0.9568760 0.88723374
location
            484.2787
                      1747 0.2772059
                                     1.0746844 0.02092398
error
           3604.7348 13975 0.2579417
$typeIII
                 SSQ
                        df
                                  MS
                                             F
Intercept
           2026.3657
                      1747 1.1599117 4.4967985 0.00000000
UICC.stage
           461.6535
                     1747 0.2642550 1.0244760 0.24661362
                      1747 0.2468253 0.9569038 0.88708056
            431.2039
sex
location
            484.2787
                     1747 0.2772059 1.0746844 0.02092398
           3604.7348 13975 0.2579417
error
```

### Adjustment by using a different parameter for every gene

In the last approach using the model  $xx=zz\beta$  for adjustment, the parameter vector  $\beta$  is estimated on a gene-wise basis. This adjustement can be selected by additionally setting the option zz.per.gene=TRUE. However, the biological meaning of this model seems unclear.

```
> GlobalAncova.decomp(xx = colon.tumour, formula = formula,
+ model.dat = colon.pheno, method = "all", zz = colon.normal,
+ zz.per.gene = TRUE)
```

### \$adjustment

ssq df adjustment 2021963 1747

### \$sequential

	SSQ	df	MS	F	р
Intercept	5.552879	1747	0.003178522	0.01076723	1.0000000
UICC.stage	370.891238	1747	0.212301796	0.71917107	1.0000000
sex	437.010911	1747	0.250149348	0.84737942	0.9999962
location	486.723097	1747	0.278605093	0.94377309	0.9428552
error	3610.043251	12229	0.295203471	NA	NA

### \$typeIII

	SSQ	df	MS	F	р
Intercept	222.9053	1747	0.1275932	0.4322213	1.0000000
UICC.stage	462.8026	1747	0.2649128	0.8973905	0.9983780
sex	436.9670	1747	0.2501242	0.8472943	0.9999962
location	486.7231	1747	0.2786051	0.9437731	0.9428552
error	3610.0433	12229	0.2952035	NA	NA

# 7 Acknowledgements

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### References

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- [2] S.R. Searle. Linear Models. Wiley, 1971.
- [3] L. J. van't Veer, H. Dai, M.J. van de Vijver, Y.D. He, A.A.M. Hart, M. Mao, H.L. Peterse, K. van der Kooy, M.J. Marton, A.T. Witteveen, G.J. Schreiber, R.M. Kerkhoven, C. Roberts, P.S. Linsley, R. Bernards, and S.H. Friend. Gene expression profiling predicts clinical outcome of breast cancer. *Nature*, 415:530–536, 2002.